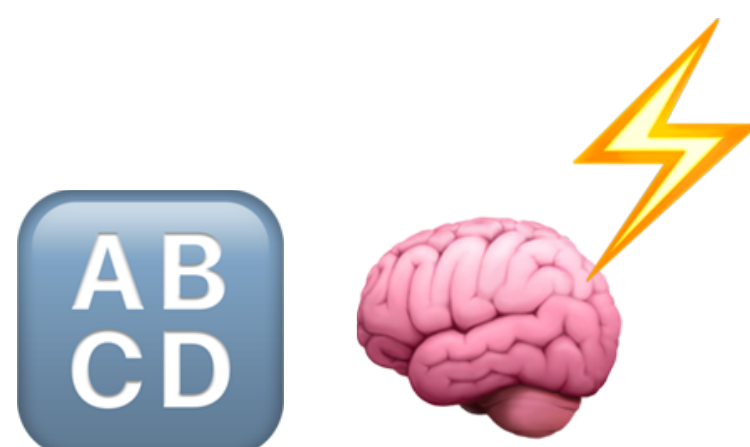


Discursive Circuits:

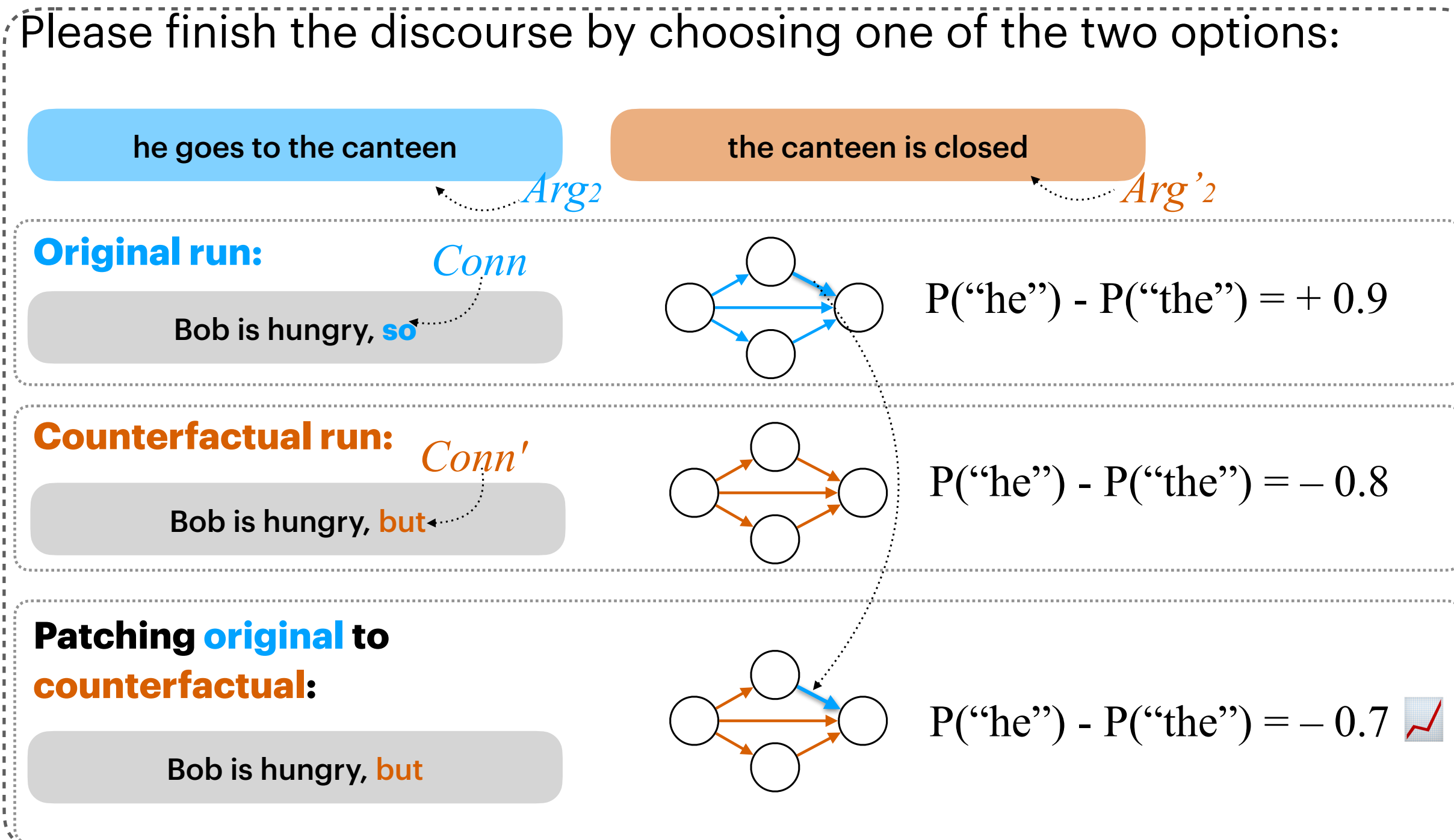
How Do Language Models Understand Discourse Relations?



Yisong Miao, Min-Yen Kan

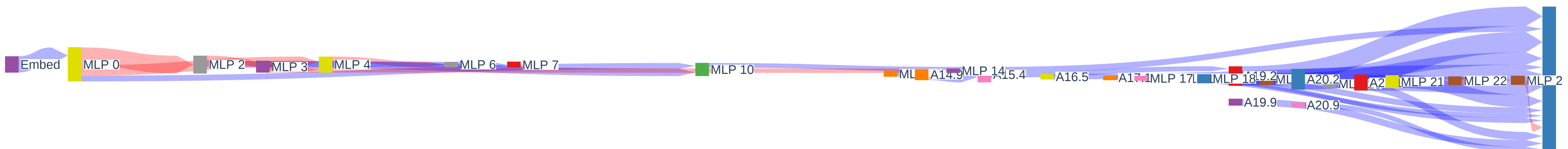
<https://github.com/YisongMiao/Discursive-Circuits>





Want to
mechanistically
interpret how LMs
understand
discourse relations?

Our Completion under Discourse Relation
(CuDR) task makes circuit discovery possible.



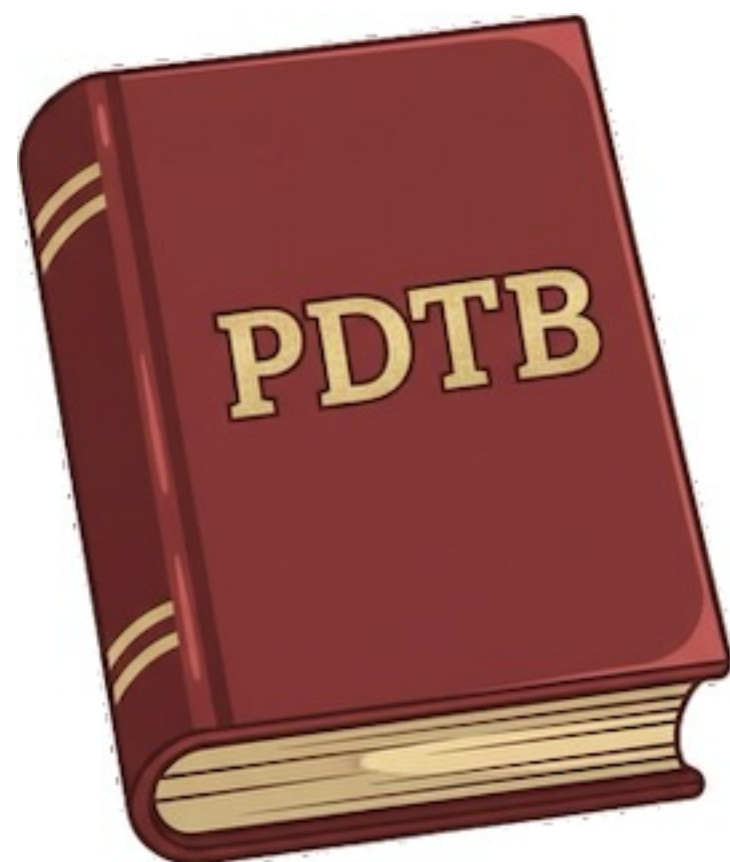
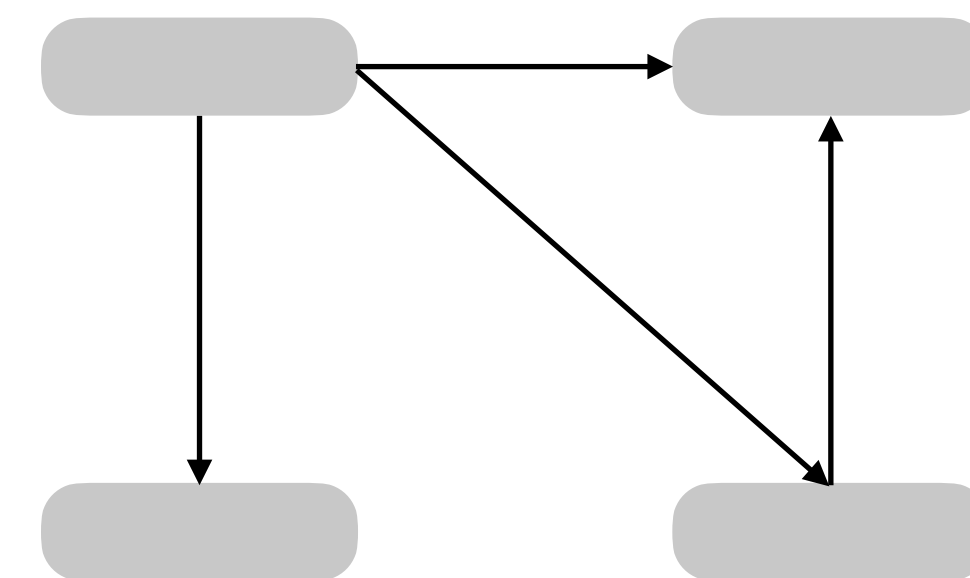
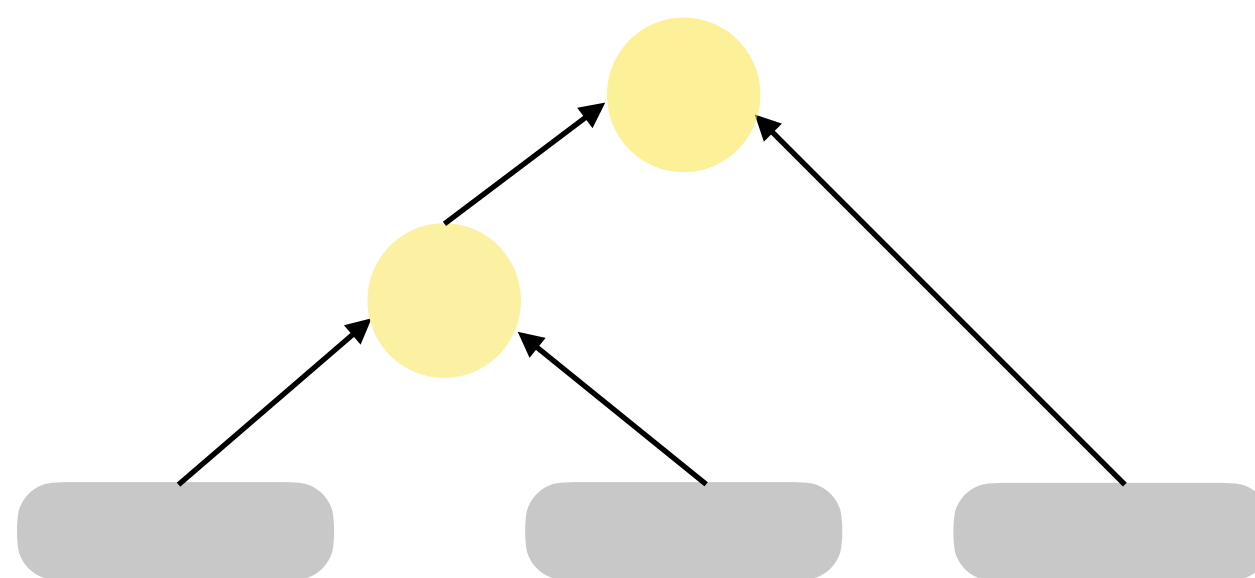
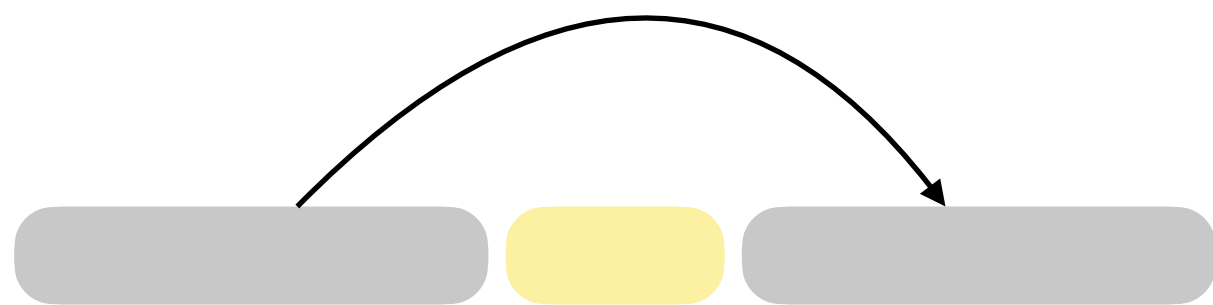
What is Discourse?

[Bob is hungry]_{Arg1} [so]_{Conn} [he goes to the canteen]_{Arg2}

[Bob is hungry]_{Arg1} [however]_{Conn} [the canteen is closed]_{Arg2}

Penn Discourse Treebank (PDTB) style discourse representation.

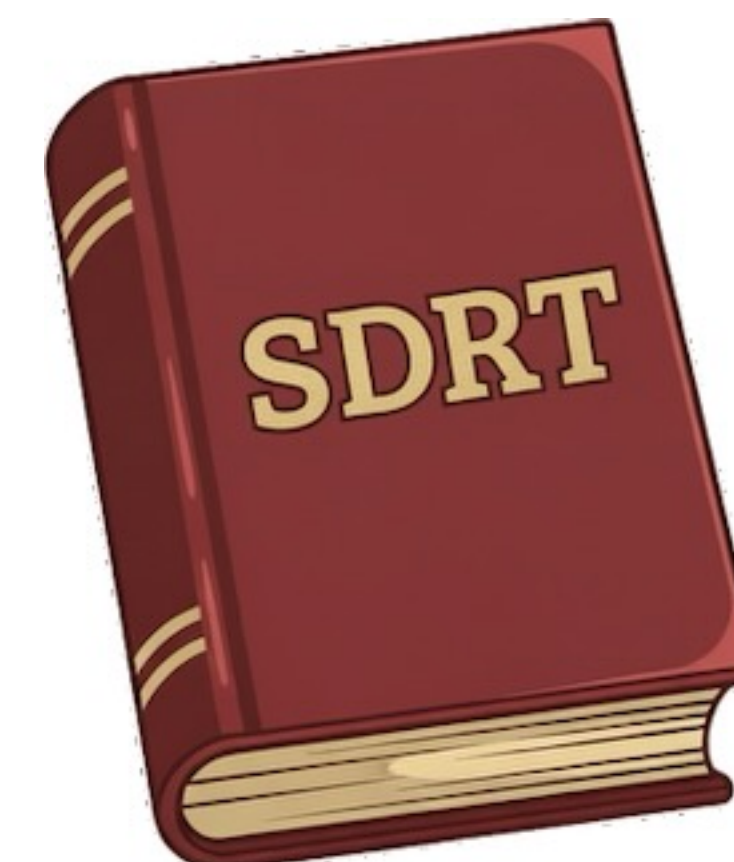
Background — Discourse



Penn Discourse Treebank

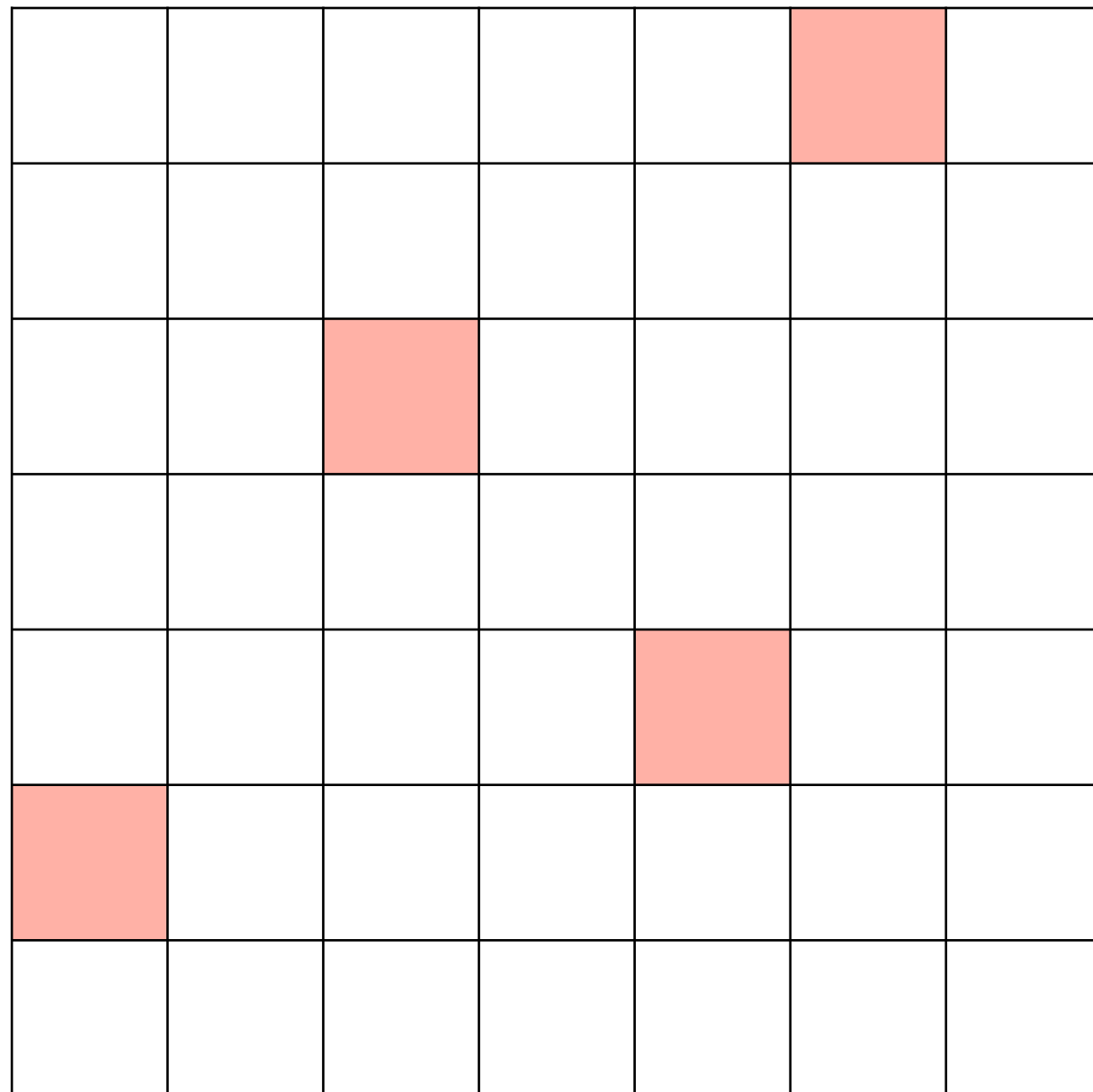


Rhetorical Structure Theory



Segmented Discourse
Representation Theory

Background — Interpretability



“Here, Bob’s action (going to the canteen) is contingent upon his state (being hungry). His hunger provides the reason for his action.”

— GPT5’s explanation.

“Attention is NOT explanation!”

(Jain and Wallace, NAACL 2019)

Are these explanations faithful?

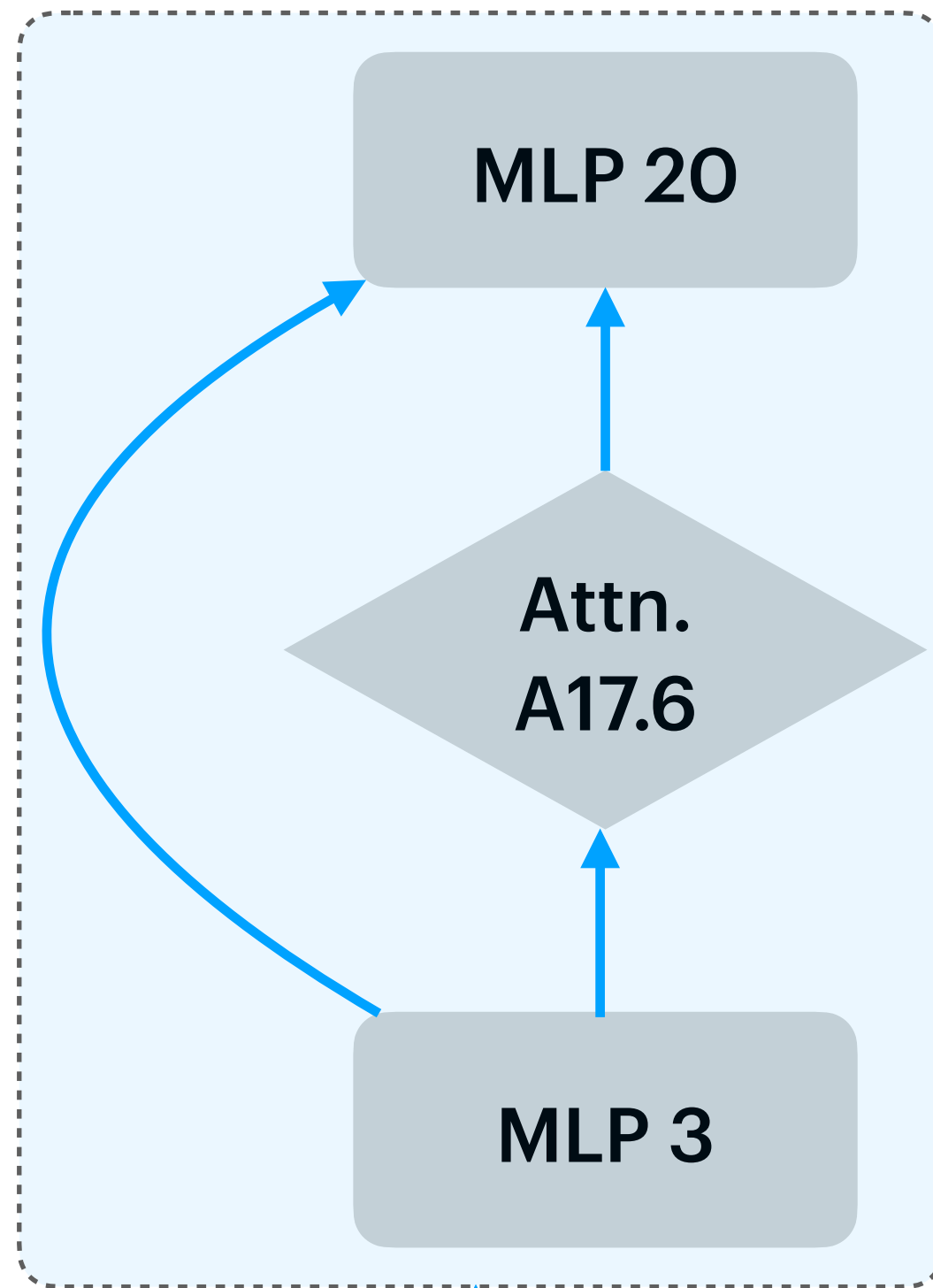
Lyu, Apidianaki, & Callison-Burch,
CL Journal 2024)

How to find the global flow of discourse in LMs?

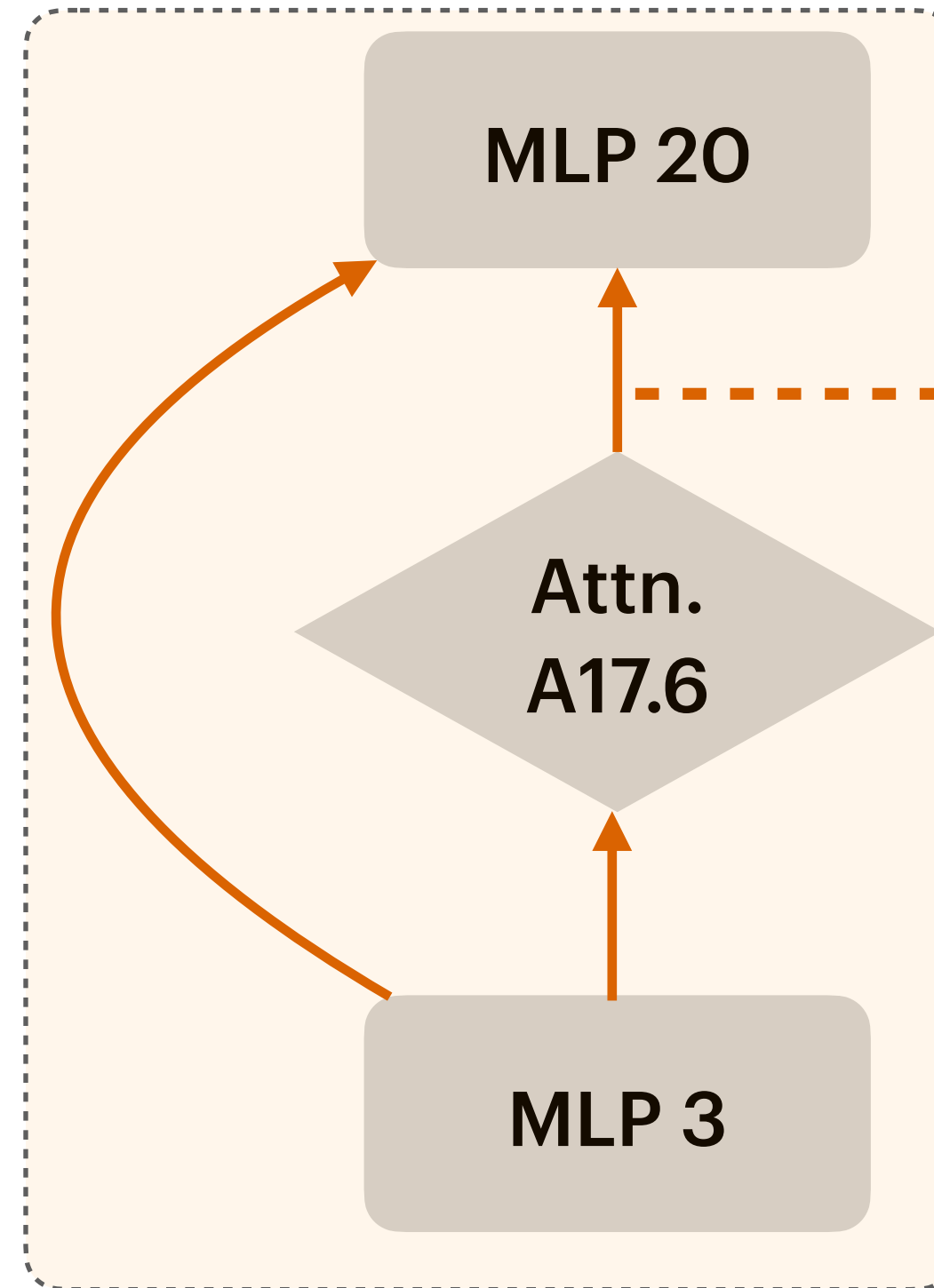


Background — Activation Patching

How to estimate an edge's importance ?

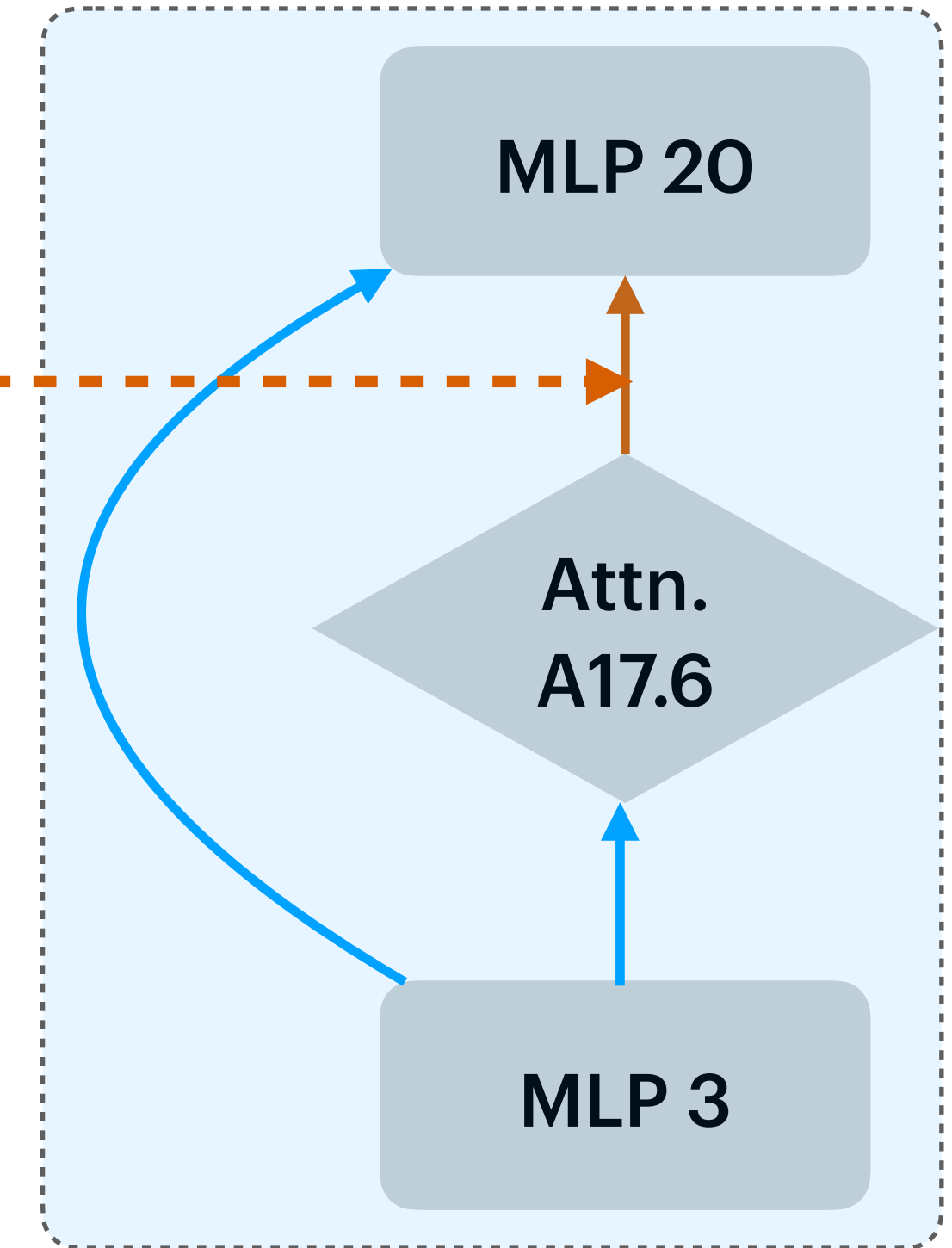


Clean run: ... 1732 to 17__
Correct answer: {33, 34, ...}



Corrupted run: ... 1701 to 17__
Correct answer: {02, 03, 04 ... }

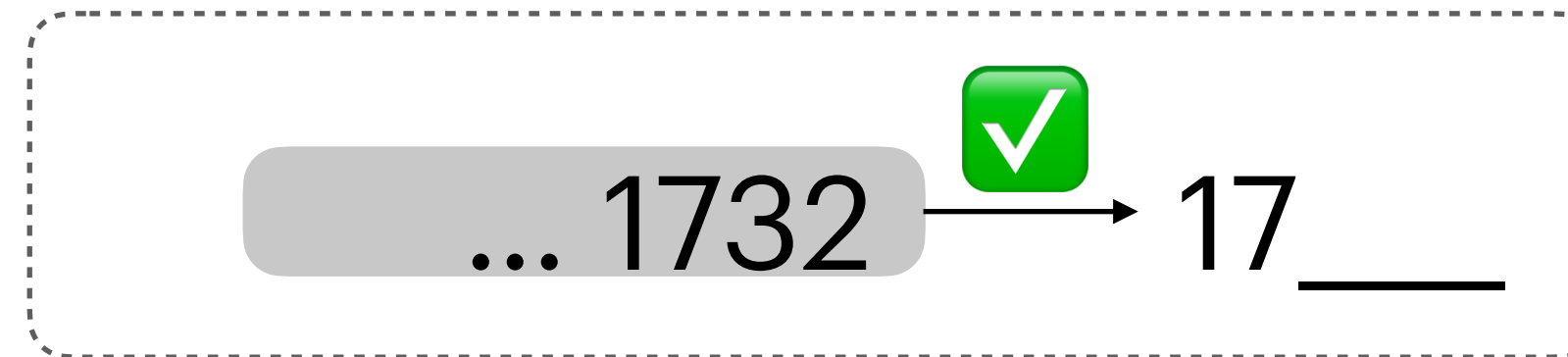
$do(e=X_{cor})$



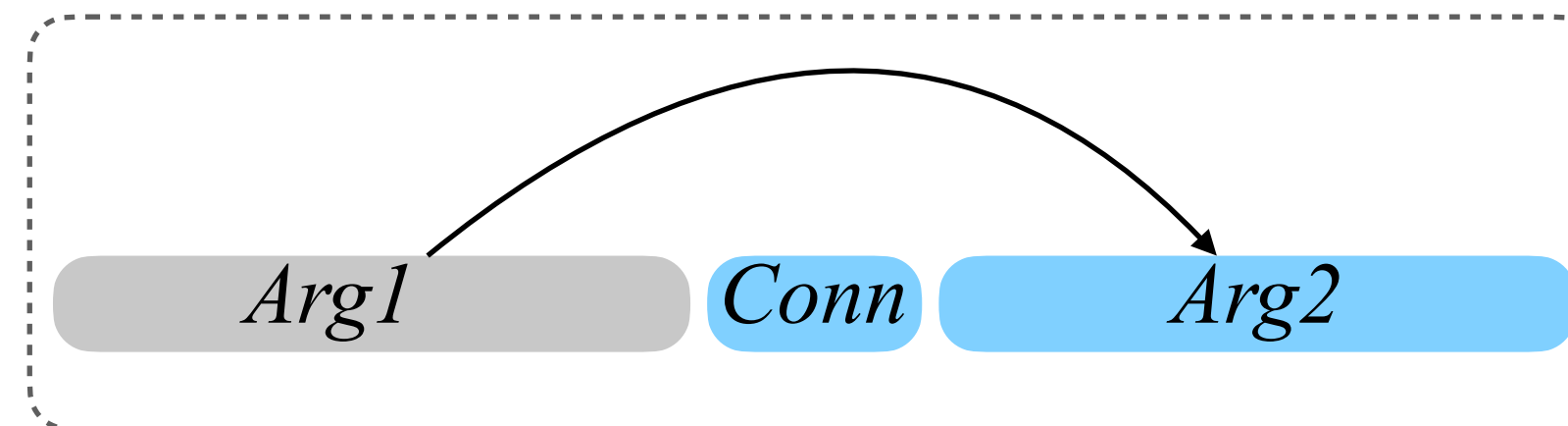
$\Delta P (y = \{33, 34, \dots\} \mid do(e=X_{cor}))$

Challenges of Discourse

“Greater-Than” relation



Discourse relations



Challenge 1: Next word prediction does not fit;

Challenge 2: No free lunch for counterfactuals;



Thesis of This Paper



Discourse Relations



Mechanistic Interpretability

Thesis of This Paper



Discourse Relations

Completion under
Discourse Relation
(CuDR)

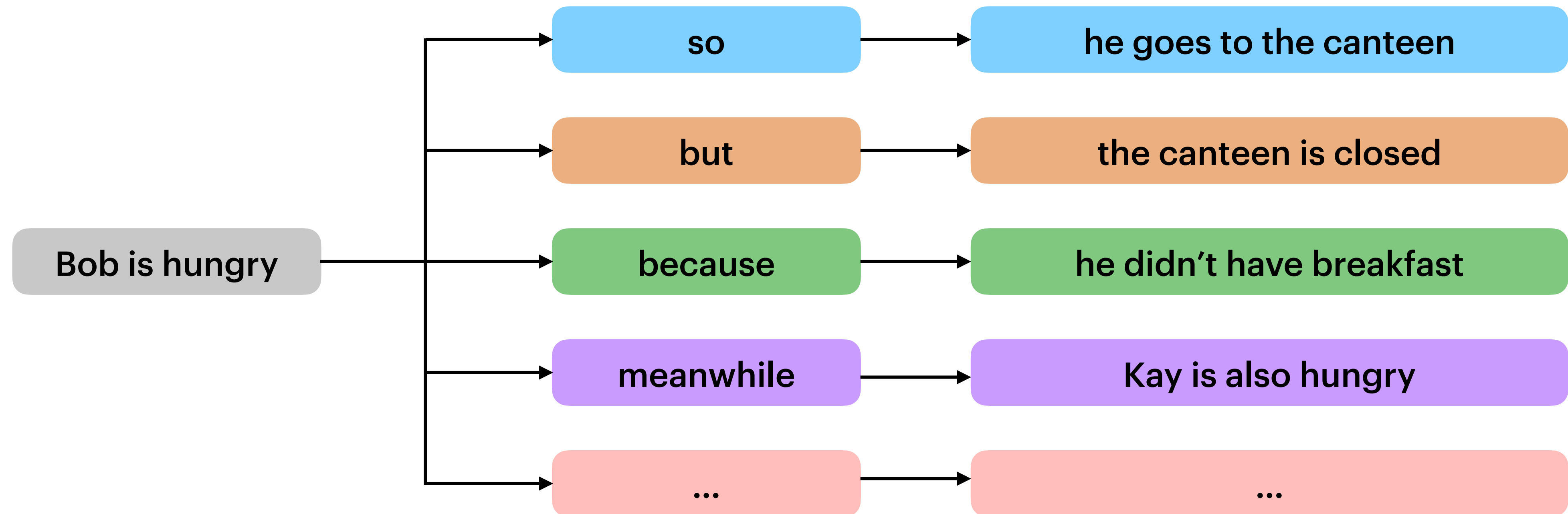


Mechanistic Interpretability

Completion under Discourse Relation

Our CuDR Task

Intuition: What **makes** us arrange the next sentence in this direction?

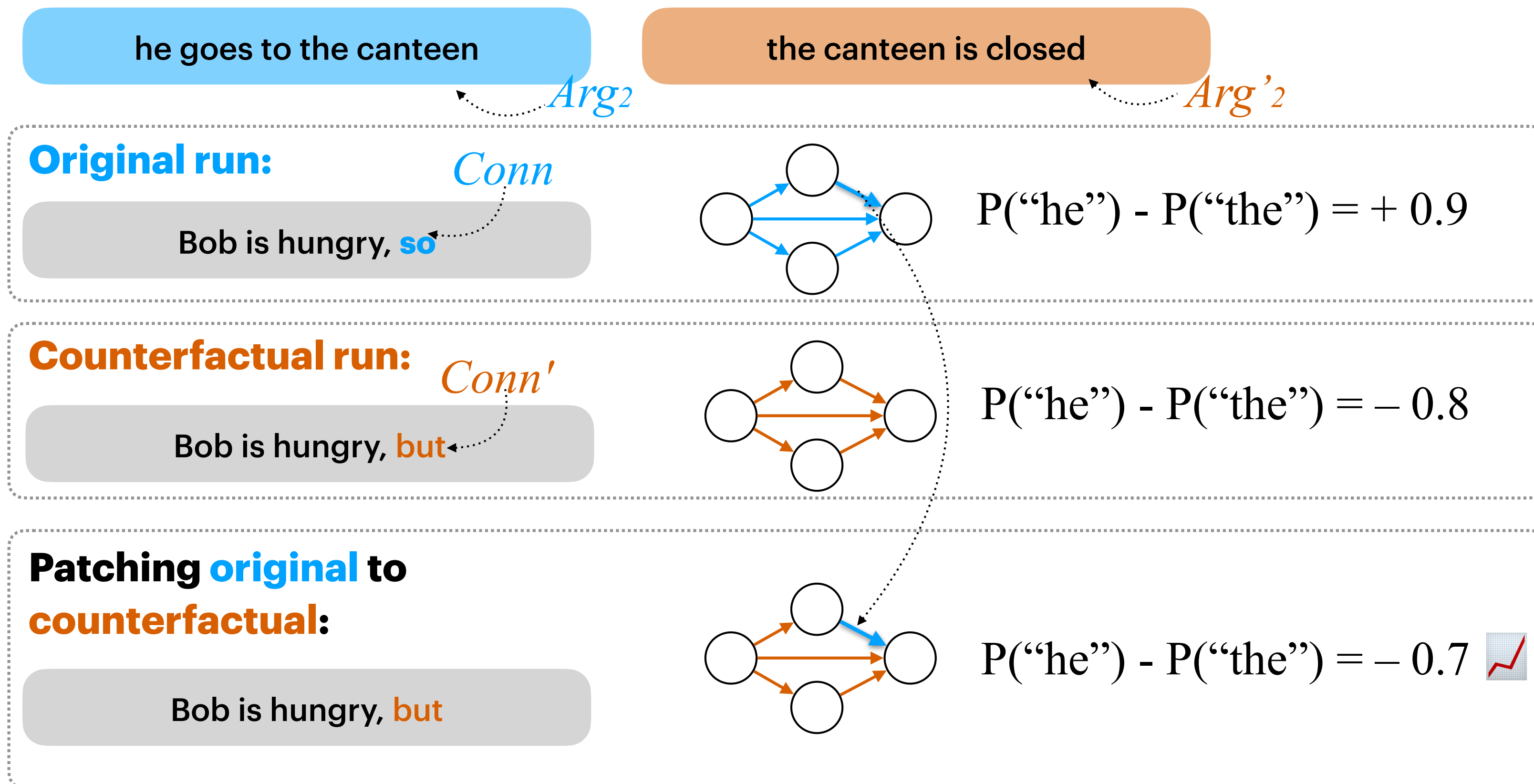


Infinite number of possible completions!

Completion under Discourse Relation

Change your mind with **minimal changes** in the input.

Please finish the discourse by choosing one of the two options:



Completion under Discourse Relation

Our CuDR Task

Input:

$d_{ori} = (Arg_1, Arg_2, R, Conn)$
 $d_{cf} = (Arg_1, Arg'_2, R', Conn')$

Activation patching:

Requirement 1: Minimal contrastive pairs;

Requirement 2: Significant change in output;

CuDR Task (Original):

Please finish the discourse by choosing one of the two options: Arg_2 or Arg'_2

To complete: $Arg_1, Conn$

Correct answer: Arg_2 , **Incorrect answer:** Arg'_2

Example: Please finish the discourse by choosing one of the two options: “he goes to the canteen” or “the canteen is closed”

To complete: $[Bob\ is\ hungry]_{Arg_1} [so]_{Conn} \Rightarrow [he\ goes\ to\ the\ canteen]_{Arg_2}$

CuDR Task (Counterfactual):

Please finish the discourse by choosing one of the two options: Arg_2 or Arg'_2

To complete: $Arg_1, Conn'$

Correct answer: Arg'_2 , **Incorrect answer:** Arg_2

Example: Please finish the discourse by choosing one of the two options: “he goes to the canteen” or “the canteen is closed”

To complete: $[Bob\ is\ hungry]_{Arg_1} [but]_{Conn'} \Rightarrow [the\ canteen\ is\ closed]_{Arg'_2}$

Activation Patching with CuDR

$$g(e) = L(x_{cf}|do(E = e_{ori})) - L(x_{cf}) \quad (1)$$

Equation (1) estimates the causal effect of any edge in the residual flow.

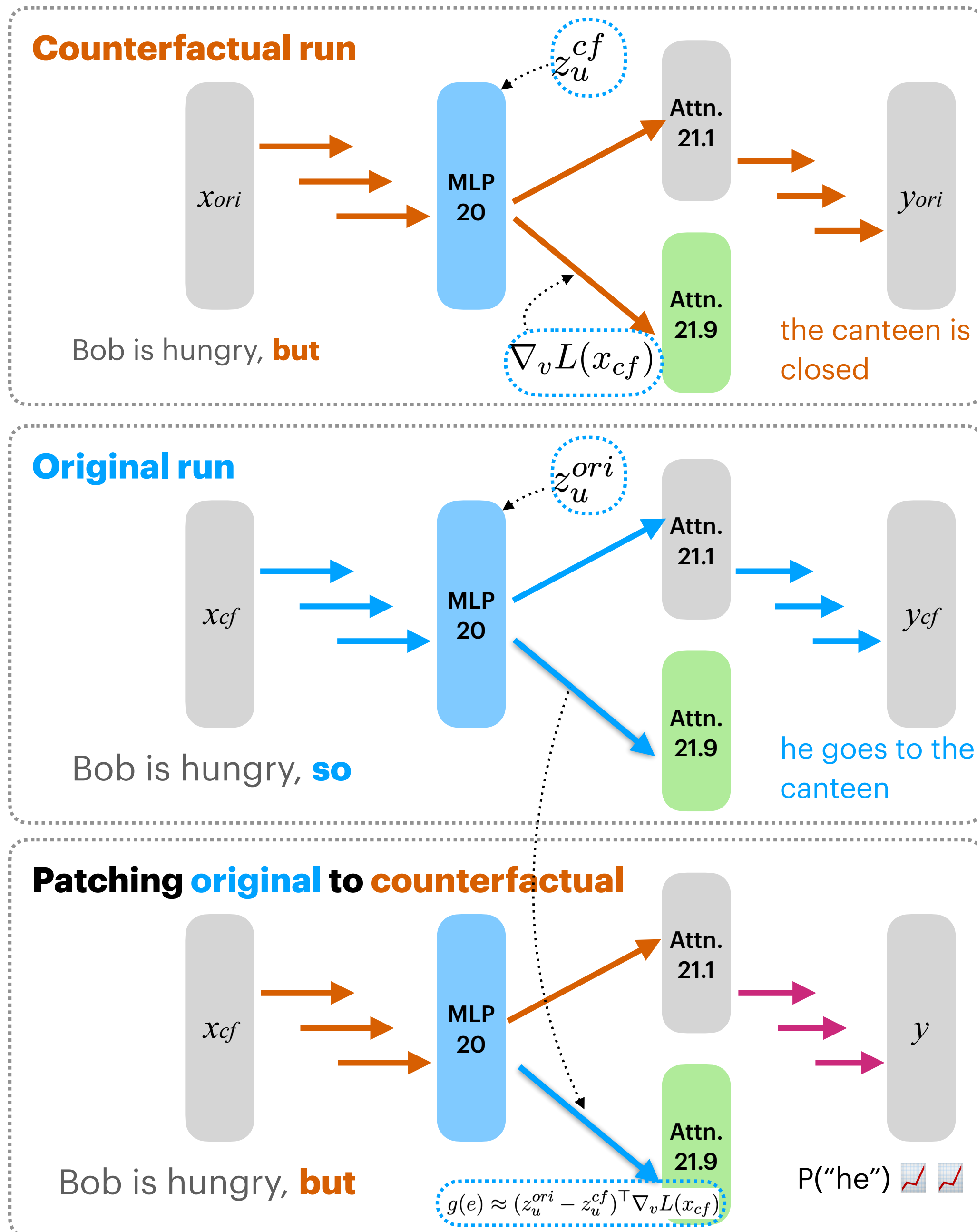
$$g(e) \approx (z_u^{ori} - z_u^{cf})^\top \nabla_v L(x_{cf}), \quad (2)$$

Equation (2) accelerates the computation by a first order Taylor approximation.

Discursive circuits are composed of top k important edges.

Reference: [Attribution patching outperforms automated circuit discovery](#). Syed, Rager, Conmy. BlackboxNLP 2024.

[Transformer circuit evaluation metrics are not robust](#). Miller, Chughtai, Saunders. COLM 2024.



Evaluation

Counterfactual CuDR data

CuDR Data Statistics

Discourse Framework	# of DR	# of CuDR data
PDTB	13	11,843
GDTB	12	5,253
GUM-RST	17	6,805
SDRT	10	3,853
Total		27,754

Original and Counterfactuals (CF)

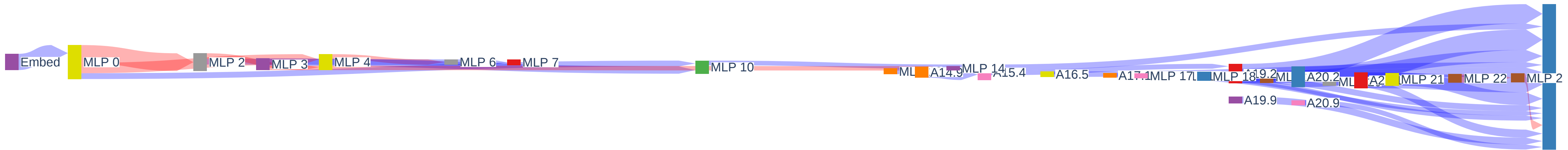
Discourse Relation	Ori Connective	CF Connectives
Comp.Conc.Arg2-as-denier	however	because for example specifically so in other words
...	...	...

Creation of CuDR Data:

- Prompt GPT 4o-mini with original *Arg₁* and a counterfactual *Conn'*.
- Each **original** discourse relation has 5 **counterfactual** relations (details in paper).

Reference: Discursive Socratic Questioning: Evaluating the Faithfulness of Language Models' Understanding of Discourse Relations. Miao, Liu, Lei, Chen, Kan. ACL 2024.

Discovering Discursive Circuit



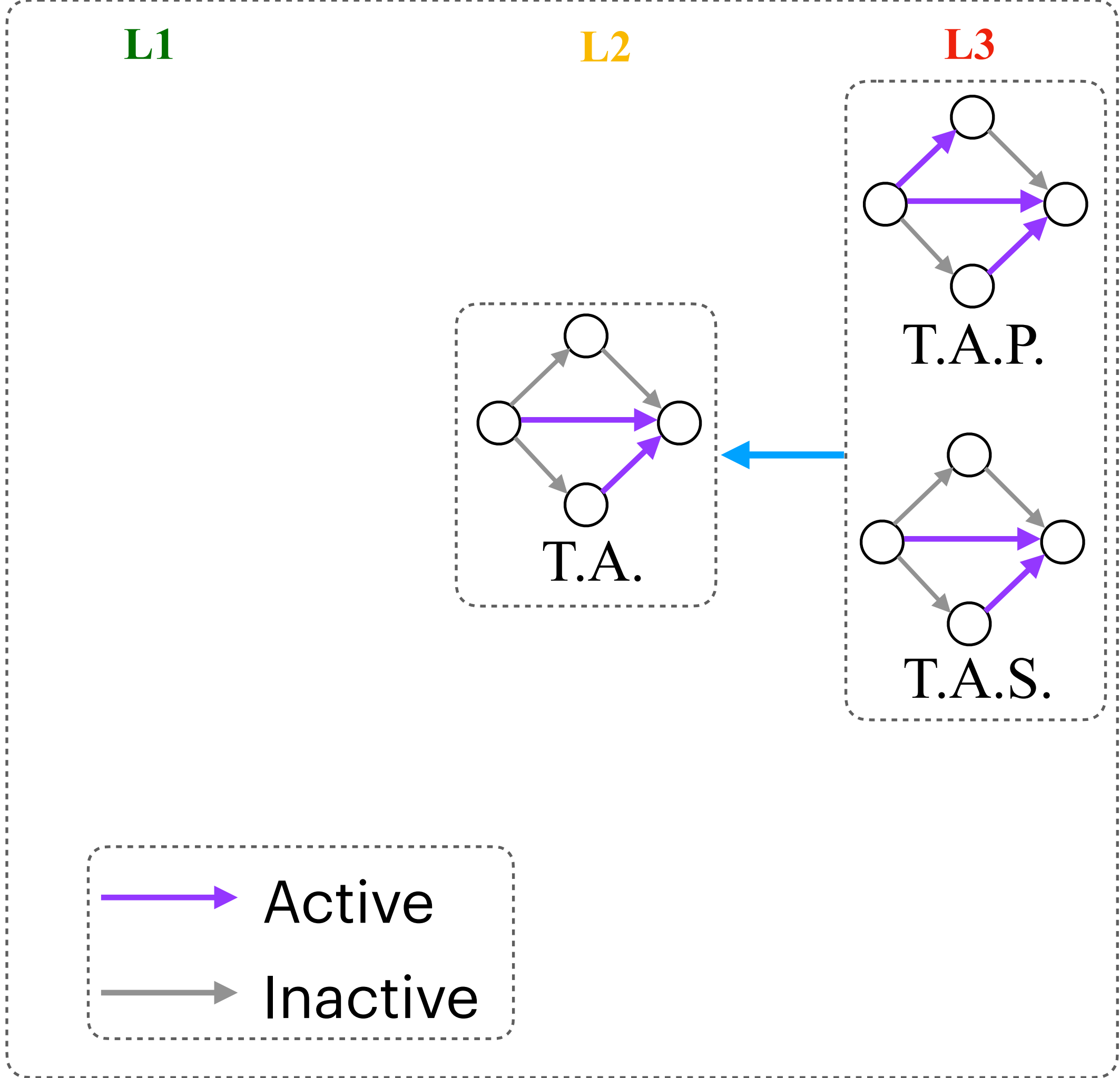
Discursive Circuits for Contingency.Result relation.

Setup:

- Sample size: 32 CuDR data (a pair of (ori, cf) instance).
- Average over 5 randomly sampled runs.

Circuit Hierarchy

A new representation of discourse.

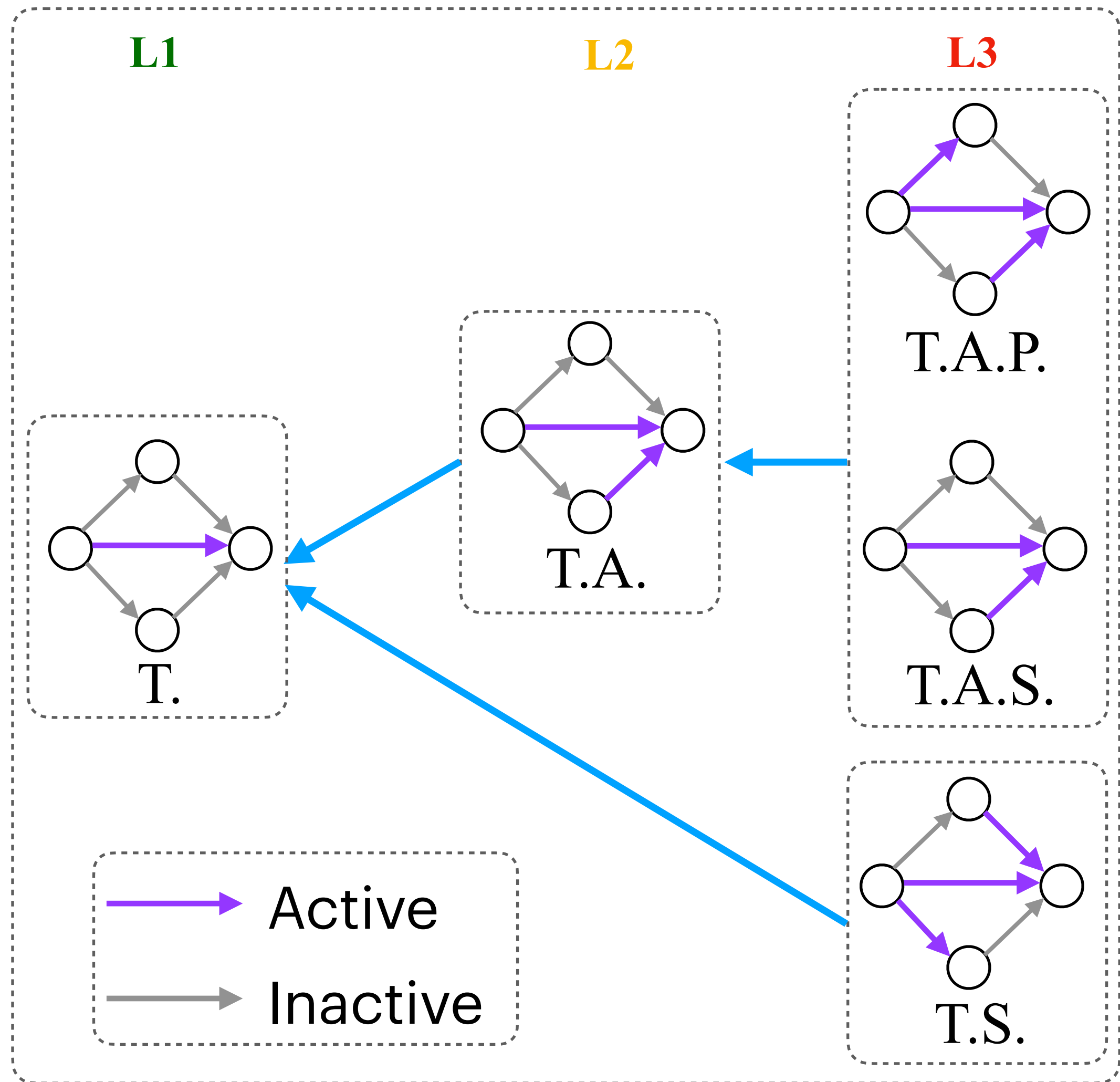


L1	L2	L3 (1000)
Comparison (568)	Concession ✗	Arg2-as-denier
	/	Contrast
Contingency (564)	/	Reason
	/	Result
	/	Conjunction
	/	Equivalence
Expansion (200)	Instantiation ✗	Arg2-as-instance
	Level-of-detail (565) ✓	Arg1-as-detail
		Arg2-as-detail
	Substitution ✗	Arg2-as-subst
Temporal (405)	<u>Asynchronous</u> (575) ✓	<u>P</u> recedence (T.A.P.)
		<u>S</u> uccession (T.A.S.)
	/	<u>S</u> ynchronous (T.S.)

$$L3 \supset L2 \supset L1 \supset L0$$

Circuit Hierarchy

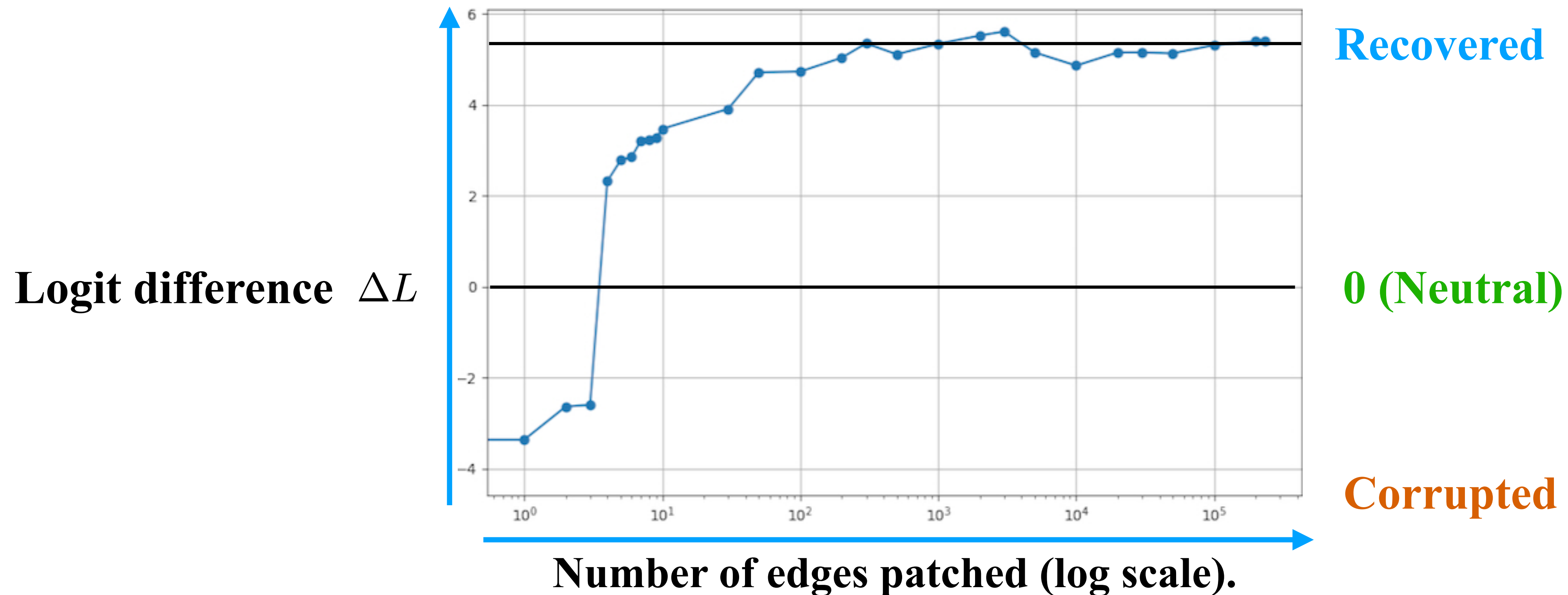
A new representation of discourse.



L1	L2	L3 (1000)
Comparison (568)	Concession ✗	Arg2-as-denier
	/	Contrast
Contingency (564)	/	Reason
	/	Result
	/	Conjunction
	/	Equivalence
Expansion (200)	Instantiation ✗	Arg2-as-instance
	Level-of-detail (565) ✓	Arg1-as-detail
		Arg2-as-detail
	Substitution ✗	Arg2-as-subst
Temporal (405)	Asynchronous (575) ✓	Precedence (T.A.P.)
		Succession (T.A.S.)
	/	Synchronous (T.S.)

$$L3 \supset L2 \supset L1 \supset L0$$

Evaluation Metric: Faithfulness Score

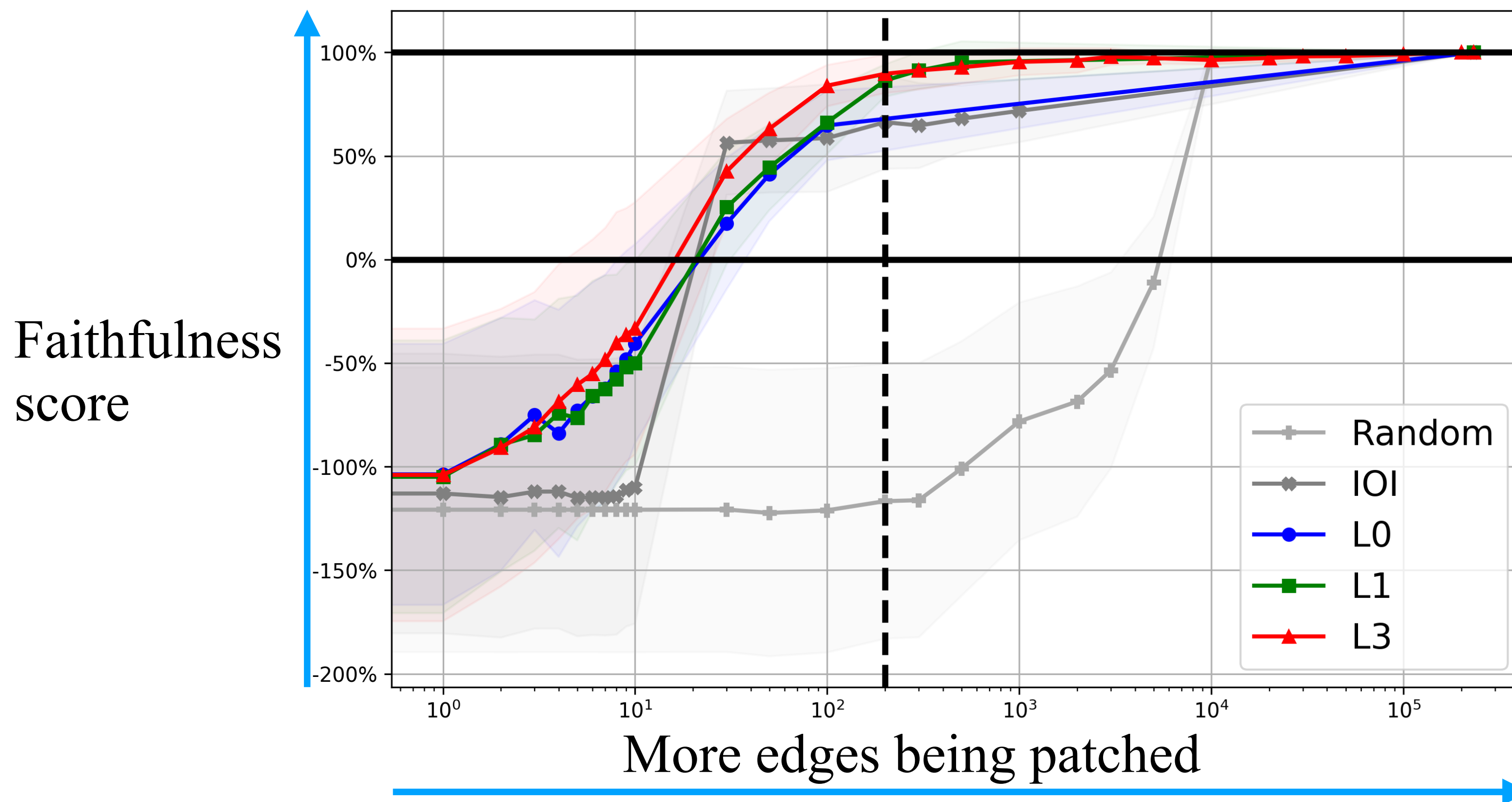


Faithfulness score:

- $\Delta L = L(Arg_2) - L(Arg'_2)$: logit difference between the two answers.
- $\frac{\Delta L_{\text{patch}}}{\Delta L_{\text{full}}}$: normalize to the full model's performance.

RQ1: Faithfulness Evaluation

Overall performance



Baseline:

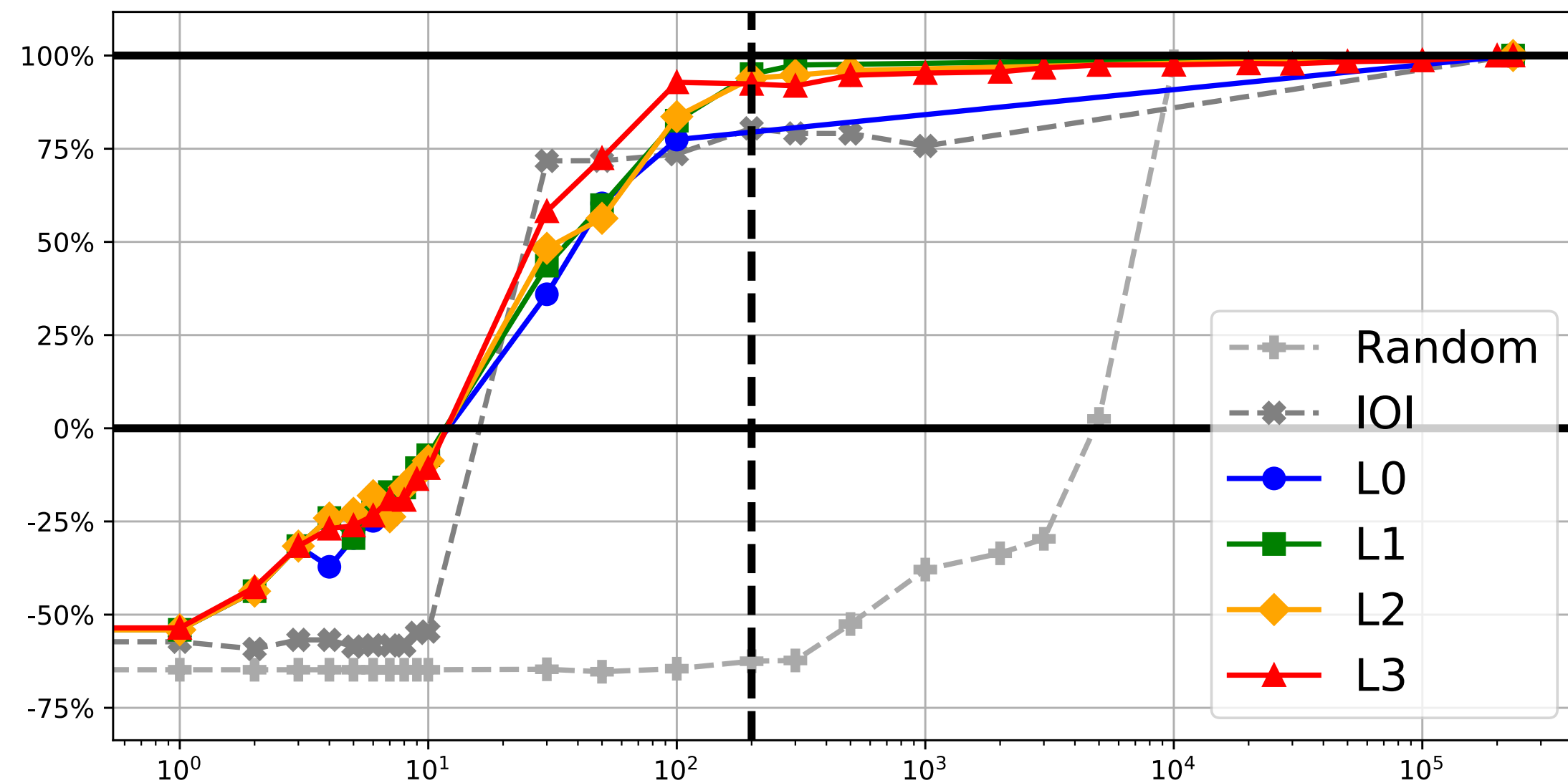
- **Random** circuits;
- **Indirect object identification (IOI)** circuits: *"Bob and Kay went to the bar, Kay gave a drink to ____"* (Answer: "Bob").

Faithfulness is recovered with around 200 edges (<0.2% of the full model).

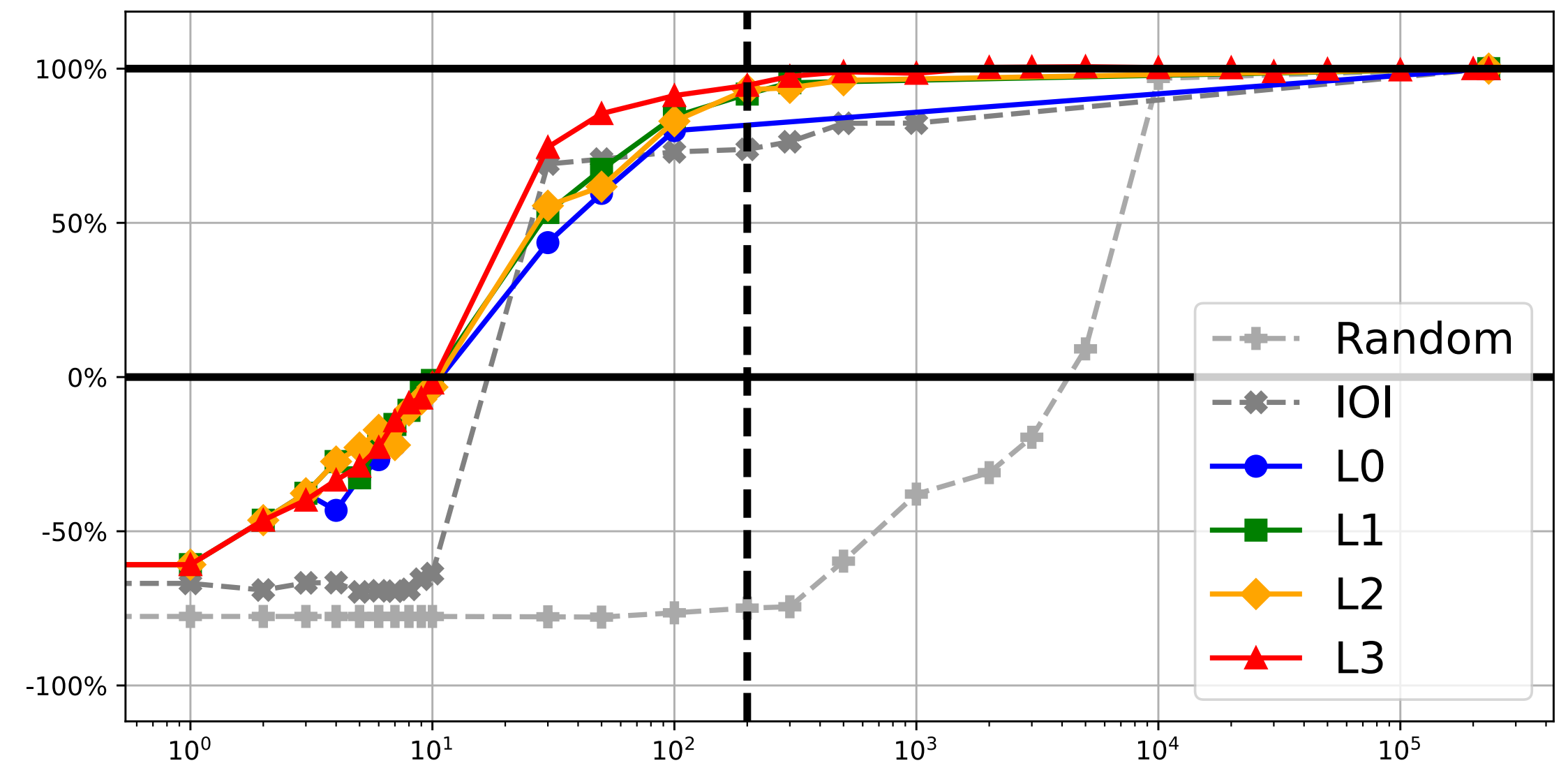
* Shadows denote variance.

RQ1: Faithfulness Evaluation

(11) Temporal.Precedence



(12) Temporal.Succession

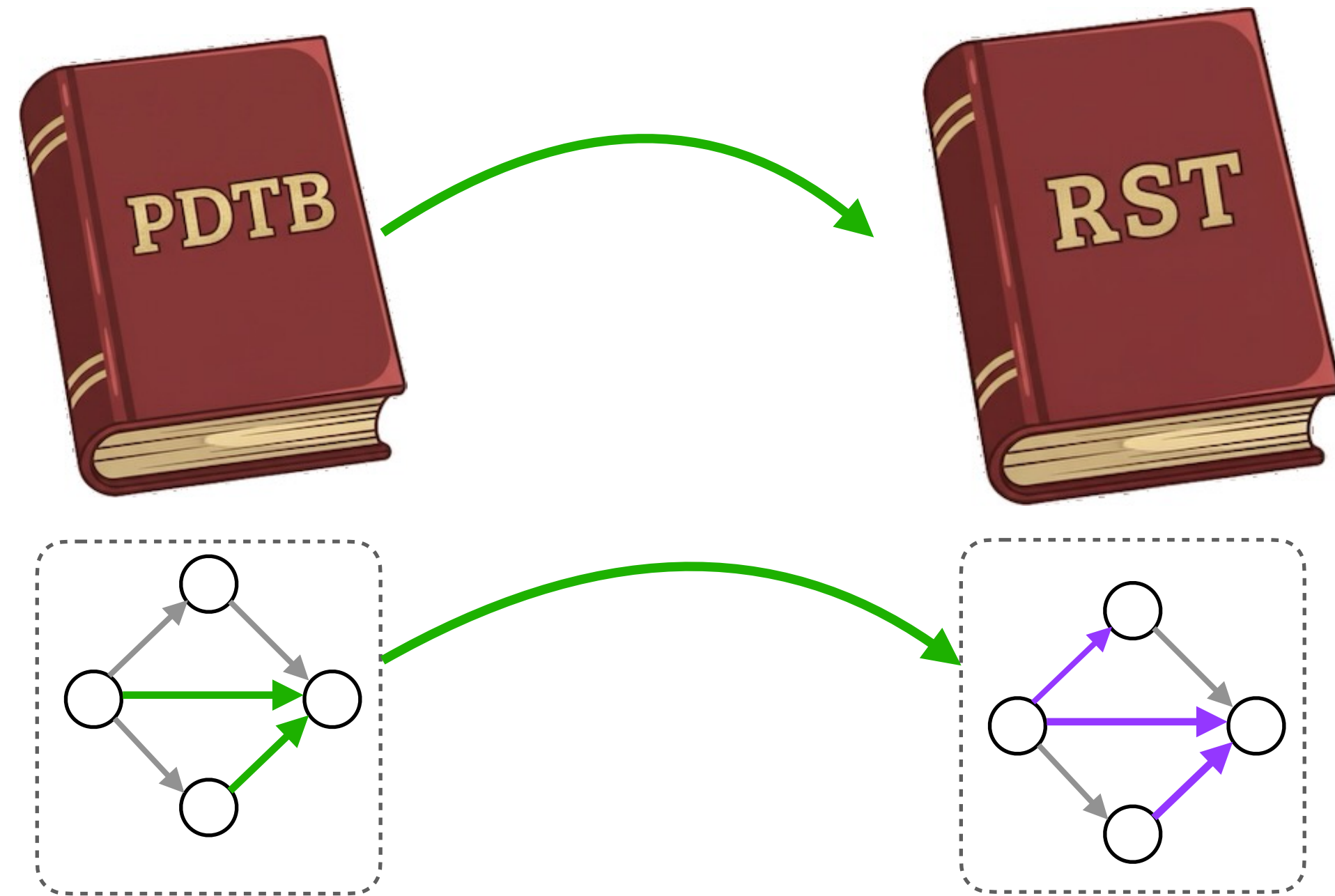


L3 > **L2** $\approx$ **L1** > **L0** > IOI >> Random

*Full results in the paper.

RQ2: Generalization Evaluation

Given discursive
circuits are exact ...

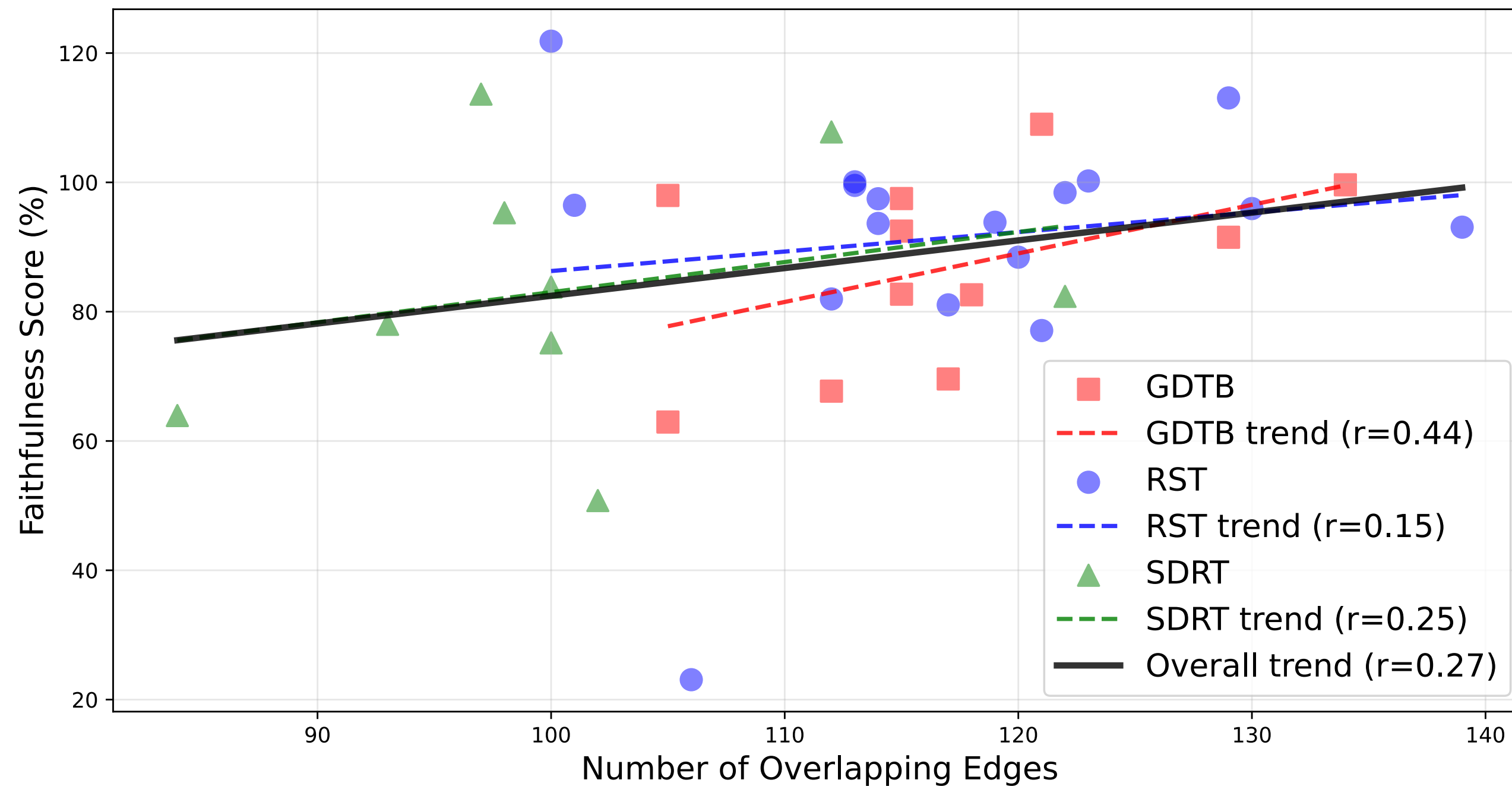


Comparison.Contrast

Adversative.Contrast

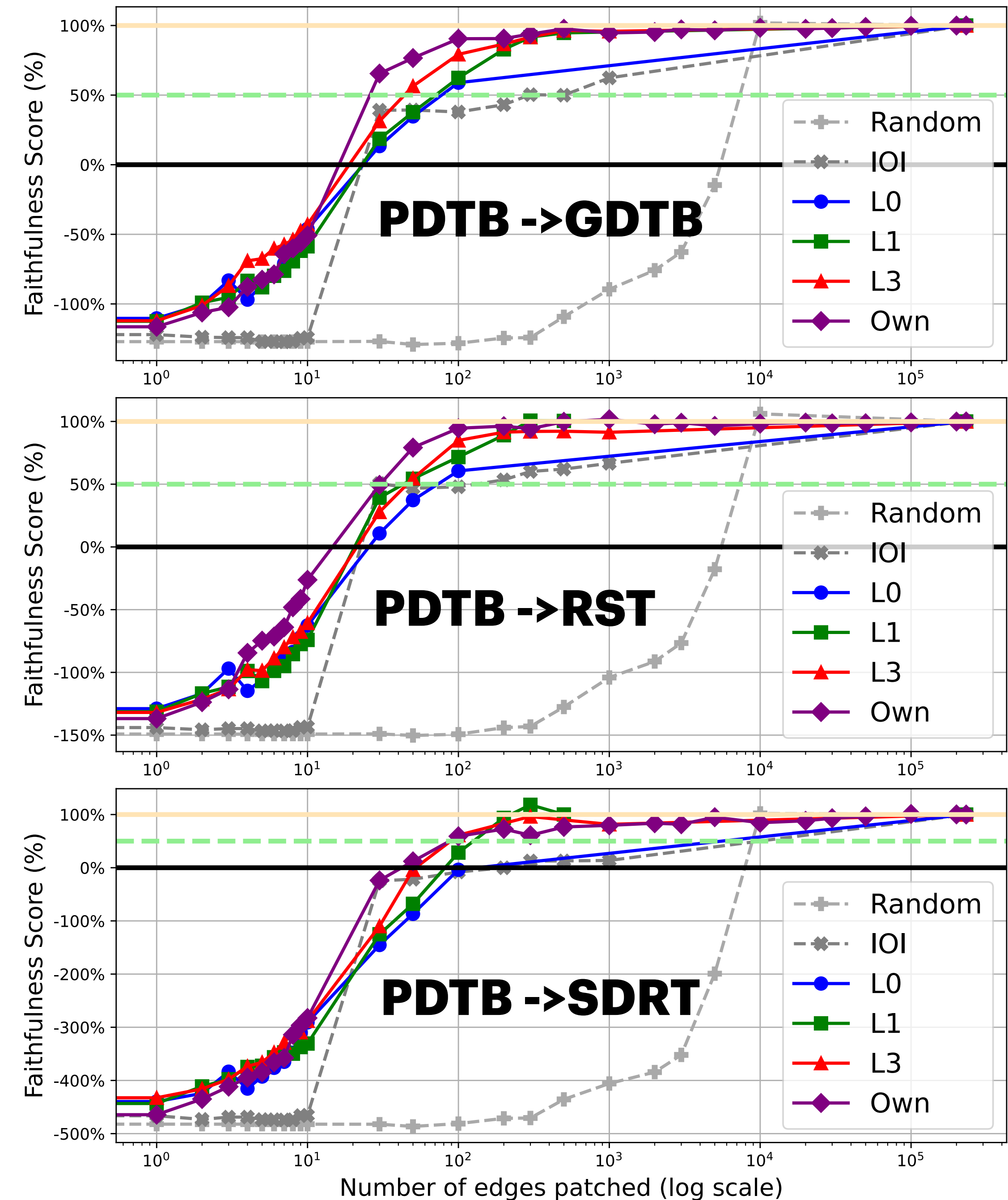
*See our paper for the full mapping among frameworks.

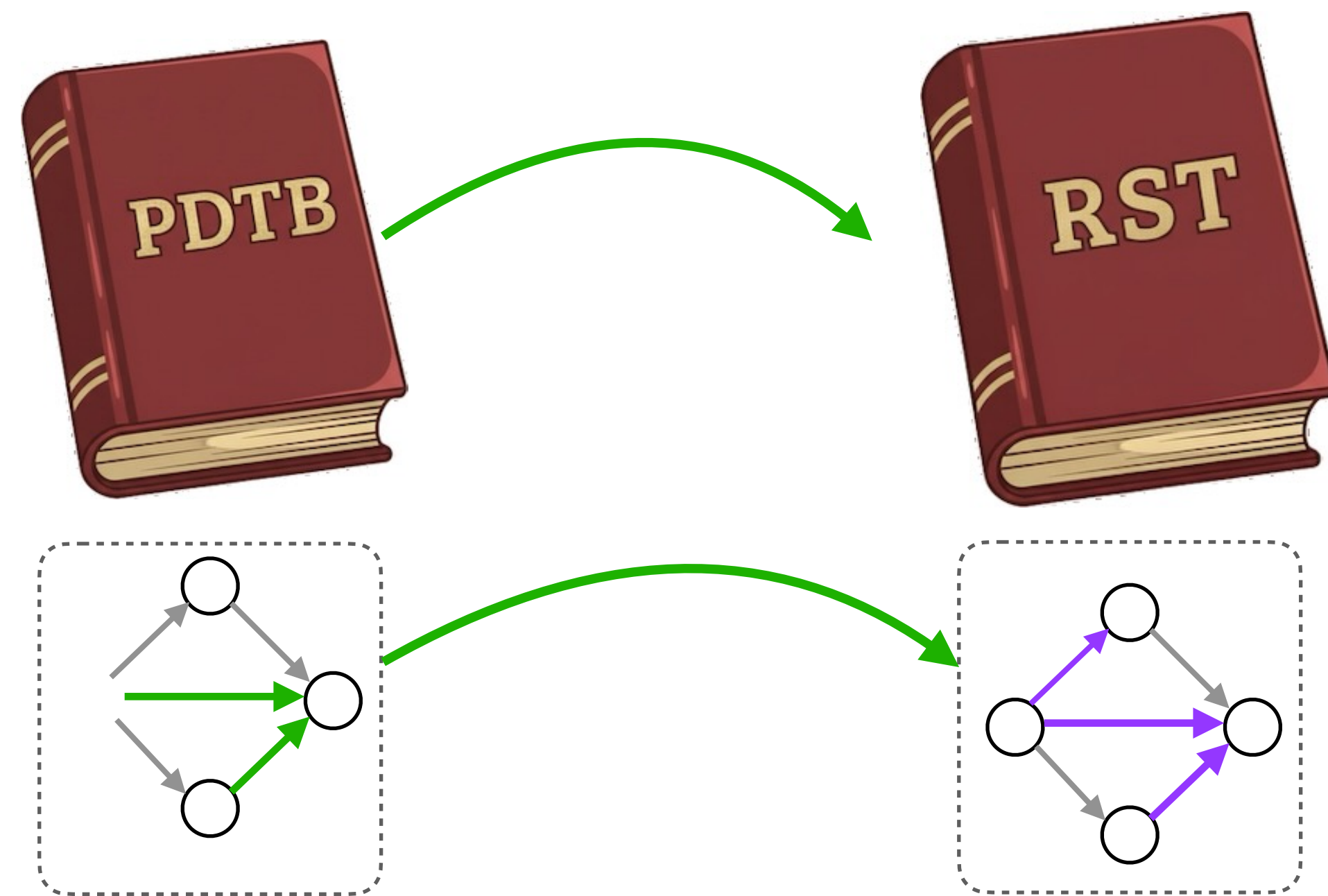
RQ2: Generalization Evaluation



Takeaway:

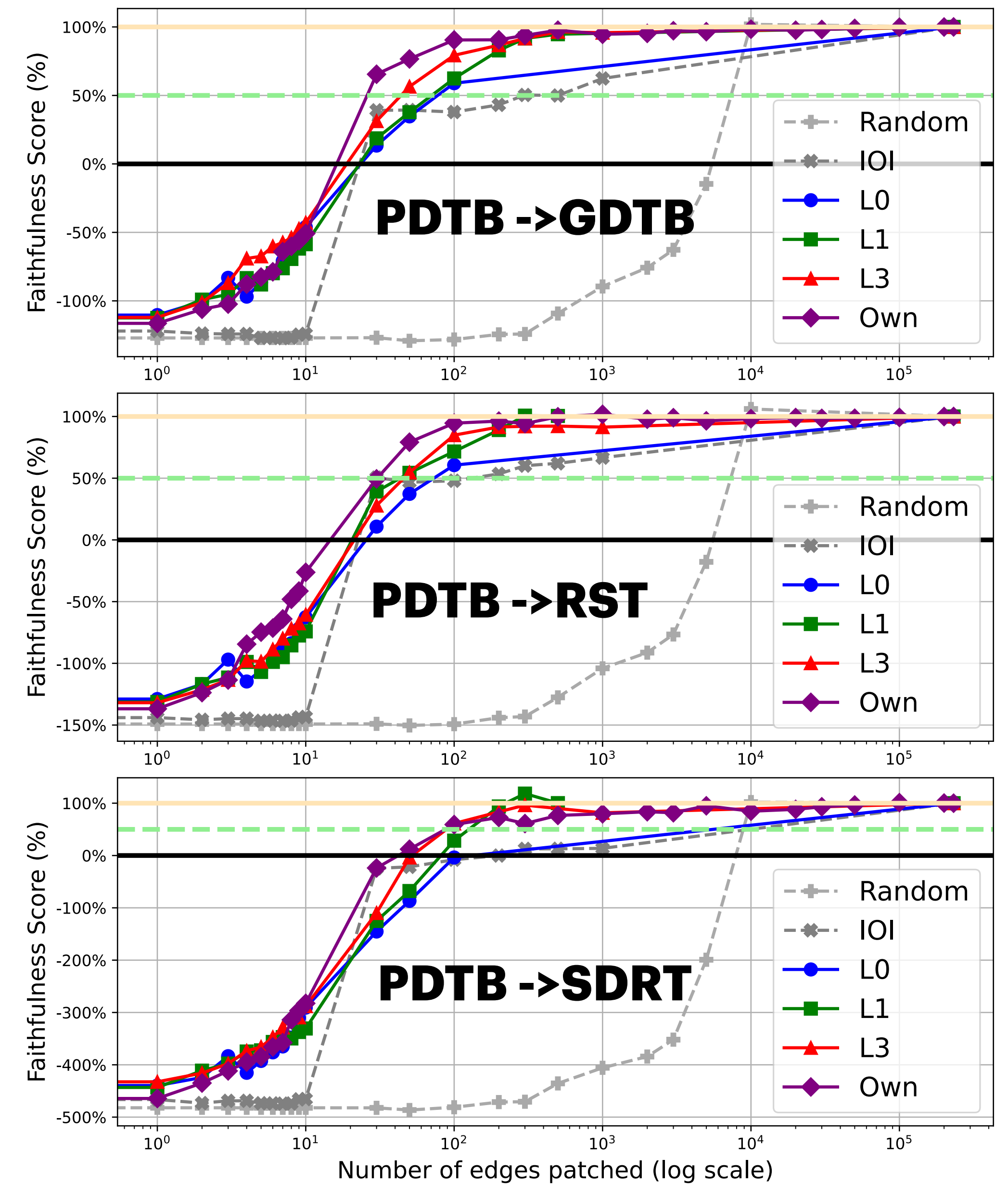
- Circuits generalize well cross-framework.
- Faithfulness $\propto$ Overlap





Comparison.Contrast

Adversative.Contrast



RQ3: Composition of linguistic features

Evaluation

Boundary words. word-pairs
Levin verb classes
Contextual features
Coreference features
Syntactic features
Named entities
Polarity / sentiment categories
Sentiment features
last three token
Modality markers
first three token
Production rules shallow parse features
Semantic features
Lexical interaction features
Numeric expressions
document position pruned/filtered
temporal expressions Negations
CFG rules
Surface features
Contextual cues neighboring relations
Verb-phrase length

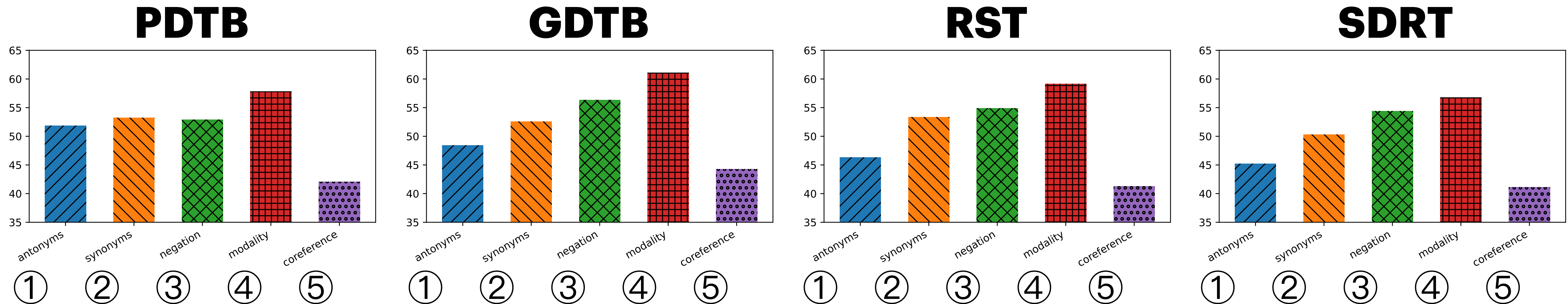
a priori?



Reference: Automatic sense prediction for implicit discourse relations in text. Pitler, Louis, Nenkova. ACL 2009.

RQ3: Composition of linguistic features

Evaluation



We consider (1) antonyms, (2) synonyms; (3) negation; (4) modality; (5) coreference.

- Utility of linguistic features: **Circuit overlaps.**
- Consistent trends of utilities among 1-5.

Conclusion

A bridge between discourse and interpretability.

New task.

Please finish the discourse by choosing one of the two options:

he goes to the canteen

the canteen is closed

Arg₂ *Arg'₂*

Original run: *Conn*

Bob is hungry, *so*

Counterfactual run: *Conn'*

Bob is hungry, *but*

Patching original to counterfactual:

Bob is hungry, *but*

$P(\text{"he"}) - P(\text{"the"}) = +0.9$

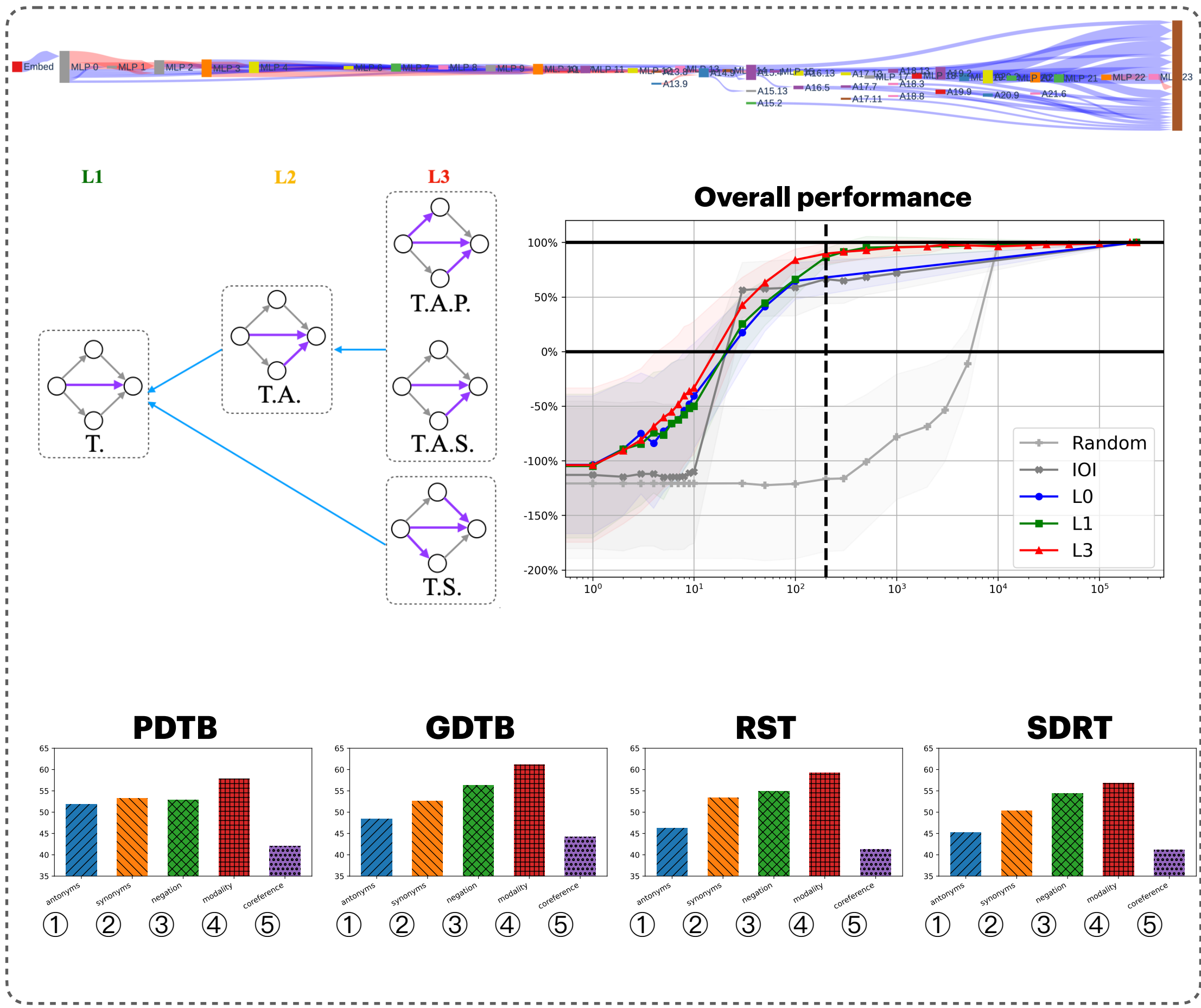
$P(\text{"he"}) - P(\text{"the"}) = -0.8$

$P(\text{"he"}) - P(\text{"the"}) = -0.7$ ✓

New datasets.

Discourse Framework	# of DR	# of CuDR data
PDTB	13	11,843
GDTB	12	5,253
GUM-RST	17	6,805
SDRT	10	3,853
Total		27,754

New representations.



Talk Feedback



<https://forms.gle/ZPV4Wc4AKYXx6Cx89>

References

- [1] Emily Pitler, Annie Louis, and Ani Nenkova. 2009. Automatic sense prediction for implicit discourse relations in text. ACL 2009.
- [2] Yisong Miao, Hongfu Liu, Wenqiang Lei, Nancy Chen, and Min-Yen Kan. 2024. Discursive socratic questioning: Evaluating the faithfulness of language models’ understanding of discourse relations. ACL 2024.
- [3] Joseph Miller, Bilal Chughtai, and William Saunders. 2024. Transformer circuit evaluation metrics are not robust. COLM 2024.
- [4] Aaquib Syed, Can Rager, and Arthur Conmy. 2024. Attribution patching outperforms automated circuit discovery. BlackboxNLP 2024.
- [5] Philipp Mondorf, Sondre Wold, and Barbara Plank. 2025. Circuit compositions: Exploring modular structures in transformer-based language models. ACL 2025.
- [6] Bonnie Webber, Rashmi Prasad, Alan Lee, and Aravind Joshi. 2019. The penn discourse treebank 3.0 annotation manual. Philadelphia, University of Pennsylvania, 35:108.
- [7] William C Mann and Sandra A Thompson. 1987. Rhetorical structure theory: A theory of text organization. University of Southern California, Information Sciences Institute Los Angeles.
- [8] Yang Janet Liu, Tatsuya Aoyama, Wesley Scivetti, Yilun Zhu, Shabnam Behzad, Lauren Elizabeth Levine, Jessica Lin, Devika Tiwari, and Amir Zeldes. 2024. GDTB: Genre diverse data for English shallow discourse parsing across modalities, text types, and domains. EMNLP 2024.
- [9] Amir Zeldes. 2017. The gum corpus: Creating multilayer resources in the classroom. Language Resources and Evaluation.
- [10] Nicholas Asher and Alex Lascarides. 2003. Logics of conversation. Cambridge University Press.
- [11] Yingxue Fu. 2022. Towards unification of discourse annotation frameworks. ACL 2022 SRW.
- [12] Florian Eichin, Yang Janet Liu, Barbara Plank, Michael A. Hedderich. 2025. Probing LLMs for Multilingual Discourse Generalization Through a Unified Label Set. ACL 2025.

Acknowledgements

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Image Credits



Baby dragons are generated with Google Gemini's image generation models.

Discourse books are also generated with Google Gemini's image generation models.



Discursive circuits are generated with Joseph Miller, Bilal Chughtai, and William Saunders's software auto-circuit.

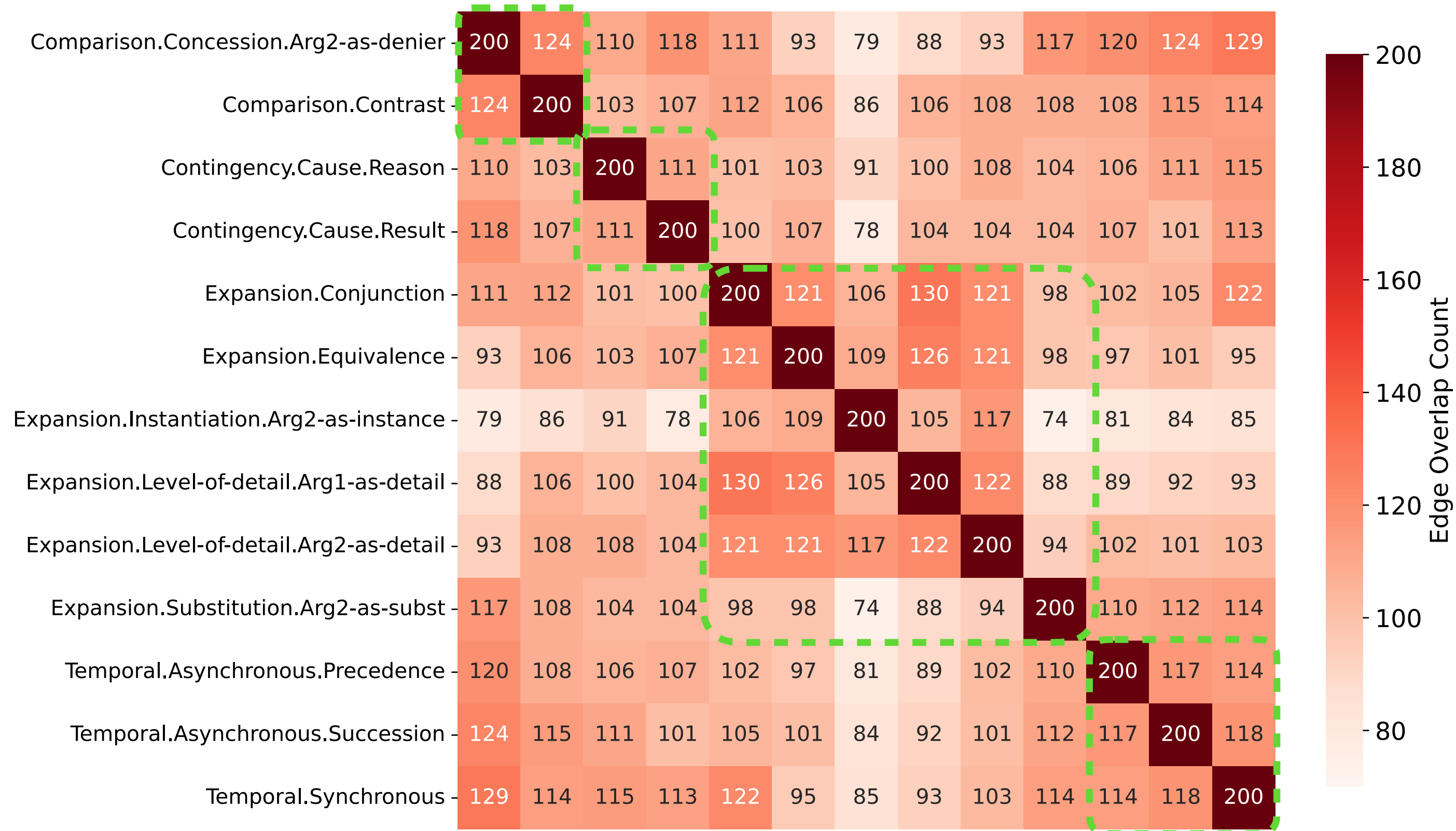
QR codes are generated with QRCode Monkey.

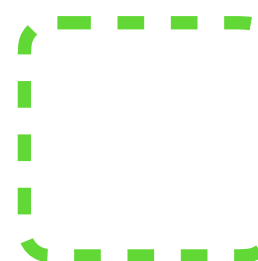


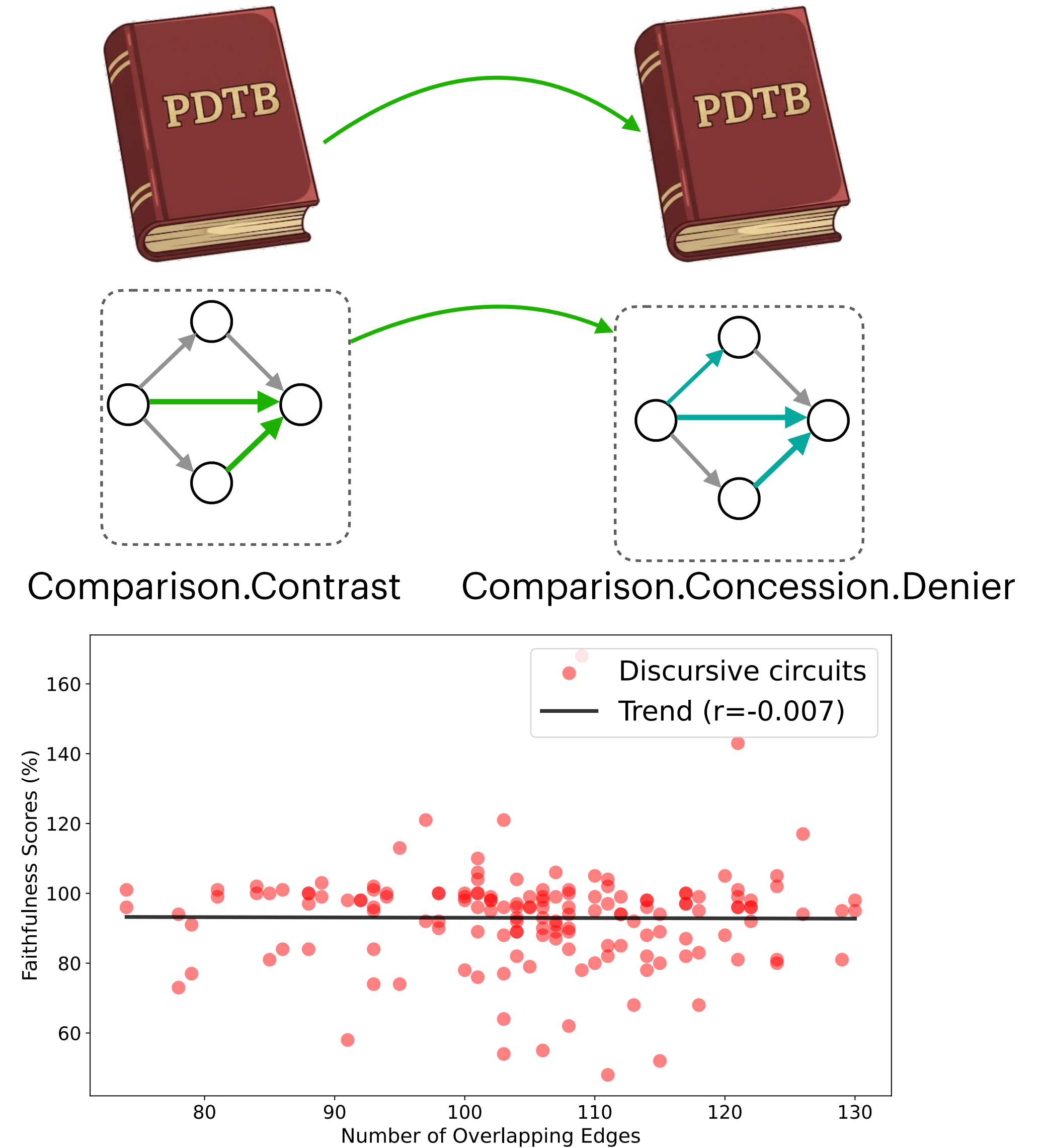
Supplementary Slides

Evaluation

RQ2: Generalization

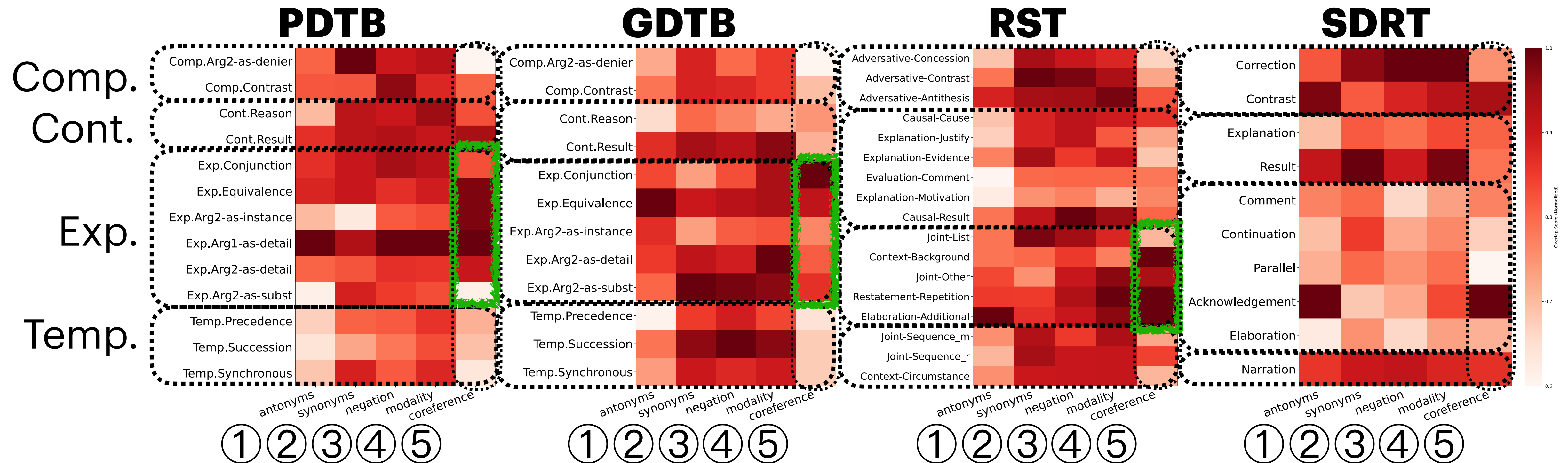


 denotes L1 clusters



Evaluation

RQ3: Composition of linguistic features



We consider (1) antonyms, (2) synonyms; (3) negation; (4) modality; (5) coreference.

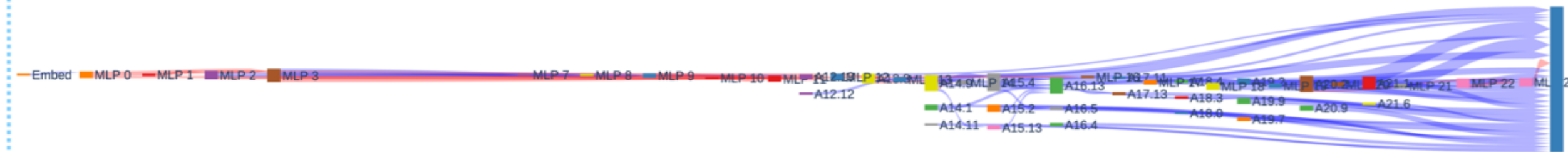
- Column-wise normalization (all columns have a **dark cell**)
- Green boundaries denote coreference-heavy zone.

Examples of Discursive Circuits

(1) PDTB: Contingency.Cause.Result



(2) GDTB: Contingency.Cause.Result



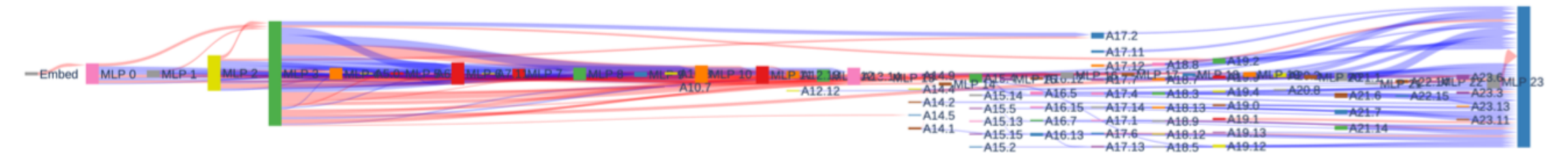
(3) RST: Cause-Result



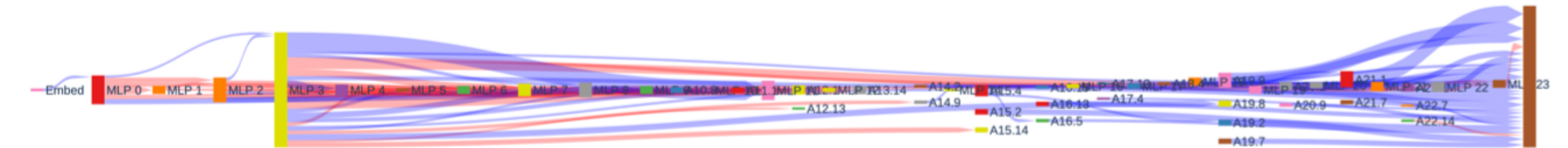
(4) SDRT: Result



(5) PDTB: Expansion.Conjunction



(6) PDTB: Expansion.Equivalence



Taylor Expansion Details

$$g(e) = L(x_{cf} \mid do(E = e_{ori})) - L(x_{cf}) \quad (1)$$

$$= L(z_u^{ori}) - L(z_u^{cf}) \quad (2)$$

$$\approx L(z_u^{cf}) + \nabla_{z_u} L(x_{cf})^\top (z_u^{ori} - z_u^{cf}) - L(z_u^{cf}) \quad (3)$$

$$= (z_u^{ori} - z_u^{cf})^\top \nabla_{z_u} L(x_{cf}) \quad (4)$$